

REAL-TIME FLUID DYNAMICS FOR GAMES

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RESEARCH

ALIAS | WAVEFRONT

PATENT

**PARTS OF THIS WORK PROTECTED
UNDER:**

US PATENT 6,266,071

MOTIVATION

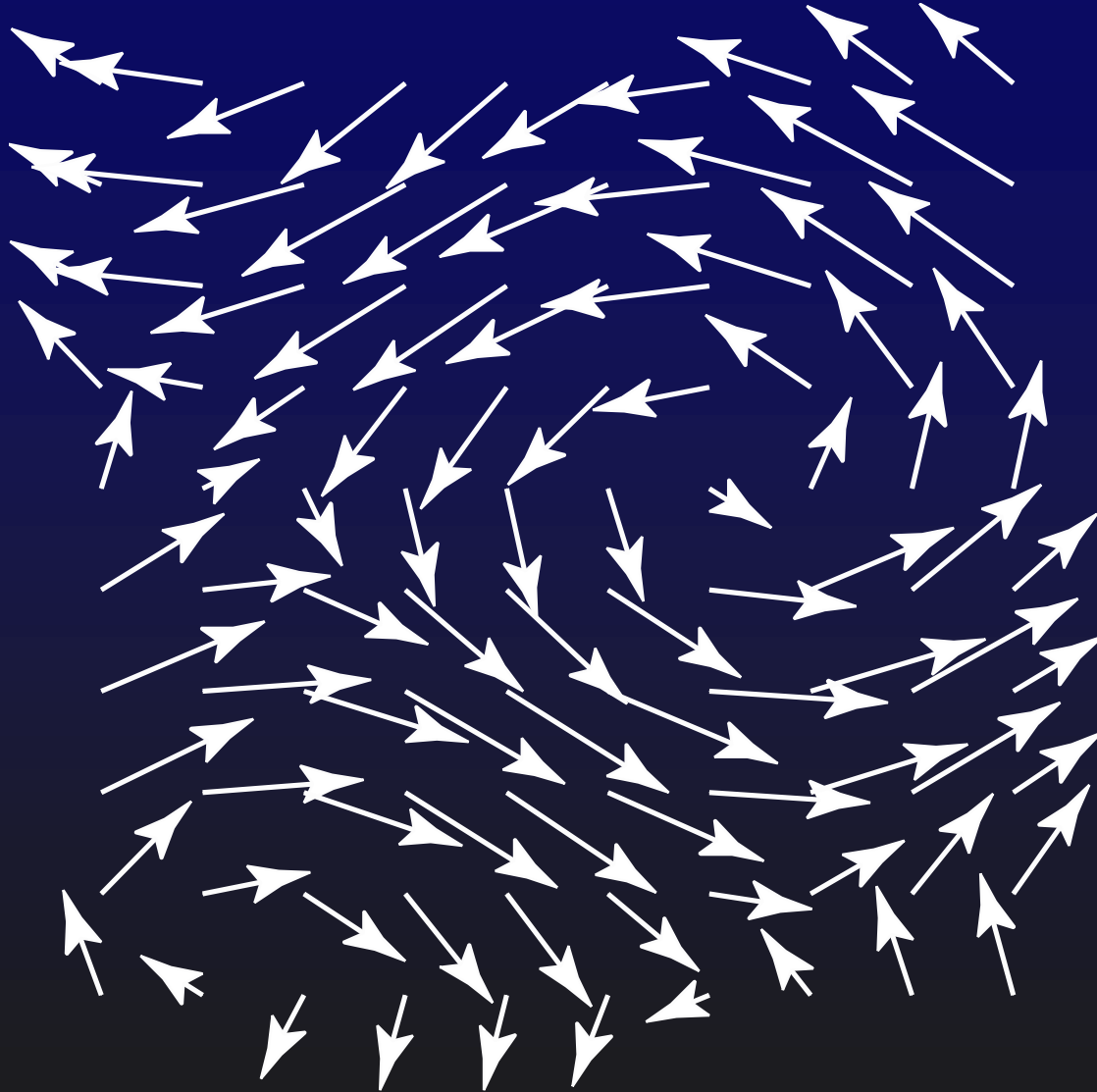
- HAS TO LOOK GOOD
- BE FAST — REAL-TIME (STABLE)
- AND SIMPLE TO CODE

IMPORTANT IN GAMES !

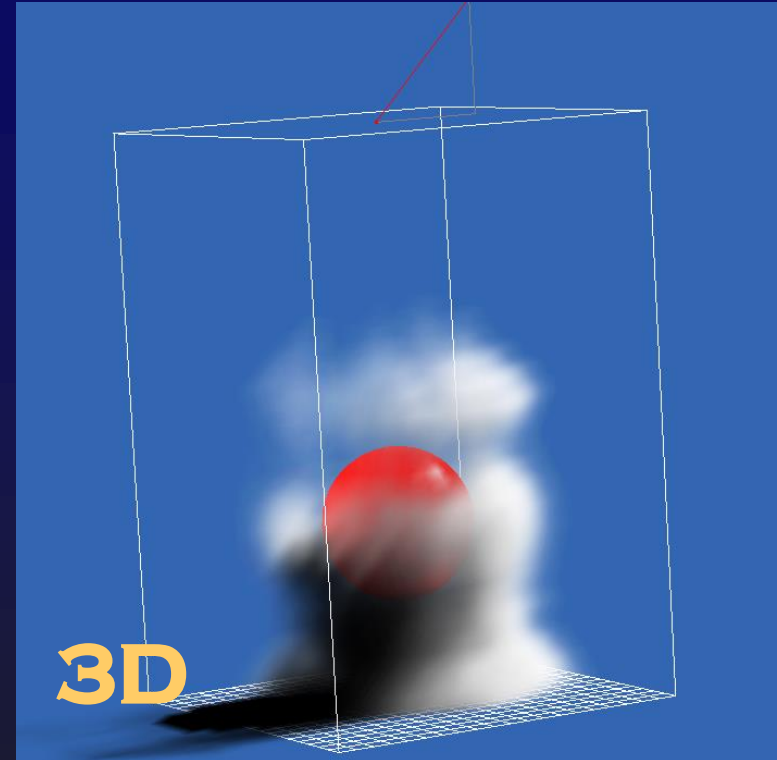
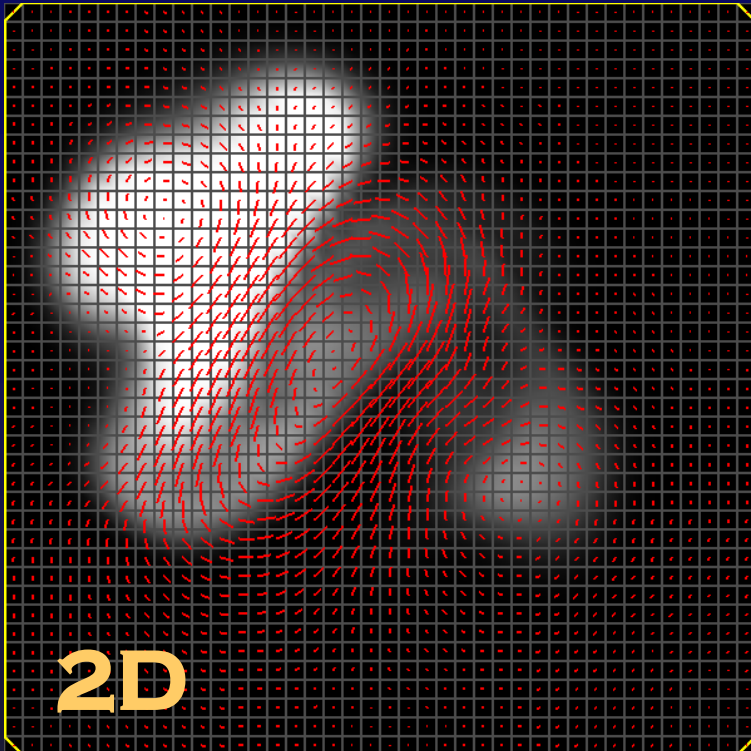
FLUID MECHANICS

- **NATURAL FRAMEWORK**
- **LOTS OF PREVIOUS WORK !**
- **VERY HARD PROBLEM**
- **VISUAL ACCURACY ?**

FLUID MECHANICS



MAIN APPLICATION



MOVING DENSITIES

MAIN APPLICATION

WHILE (SIMULATING)

GET FORCES FROM UI

GET SOURCE DENSITIES FROM UI

UPDATE VELOCITY FIELD

UPDATE DENSITY FIELD

DISPLAY DENSITY

NAVIER-STOKES EQUATIONS

$$\frac{\partial \mathbf{u}}{\partial t} = -(\mathbf{u} \cdot \nabla) \mathbf{u} + \nu \nabla^2 \mathbf{u} + \mathbf{f}$$

VELOCITY

$$\frac{\partial \rho}{\partial t} = -(\mathbf{u} \cdot \nabla) \rho + \kappa \nabla^2 \rho + S$$

DENSITY

EQUATIONS VERY SIMILAR

WHAT DOES IT MEAN ?

$$\boxed{\frac{\partial \rho}{\partial t}} = -(\mathbf{u} \cdot \nabla) \rho + \kappa \nabla^2 \rho + S$$

OVER TIME...

WHAT DOES IT MEAN ?

$$\frac{\partial \rho}{\partial t} = \boxed{-(\mathbf{u} \cdot \nabla) \rho} + \kappa \nabla^2 \rho + S$$

DENSITY FOLLOWS VELOCITY...

WHAT DOES IT MEAN ?

$$\frac{\partial \rho}{\partial t} = -(\mathbf{u} \cdot \nabla) \rho + \boxed{\kappa \nabla^2 \rho} + S$$

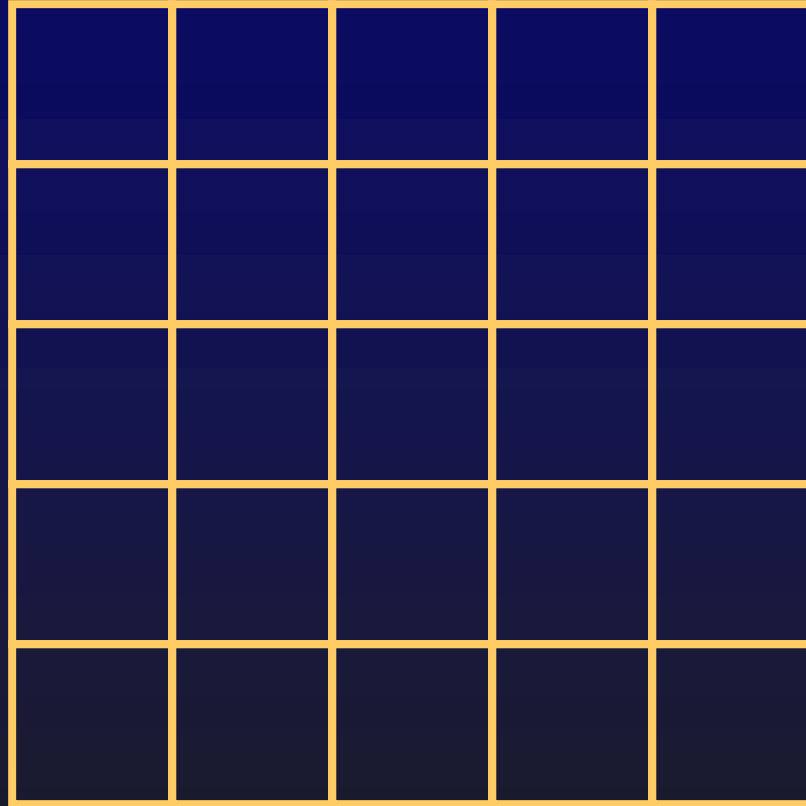
DENSITY DIFFUSES AT A RATE κ ...

WHAT DOES IT MEAN ?

$$\frac{\partial \rho}{\partial t} = -(\mathbf{u} \cdot \nabla) \rho + \kappa \nabla^2 \rho + \boxed{S}$$

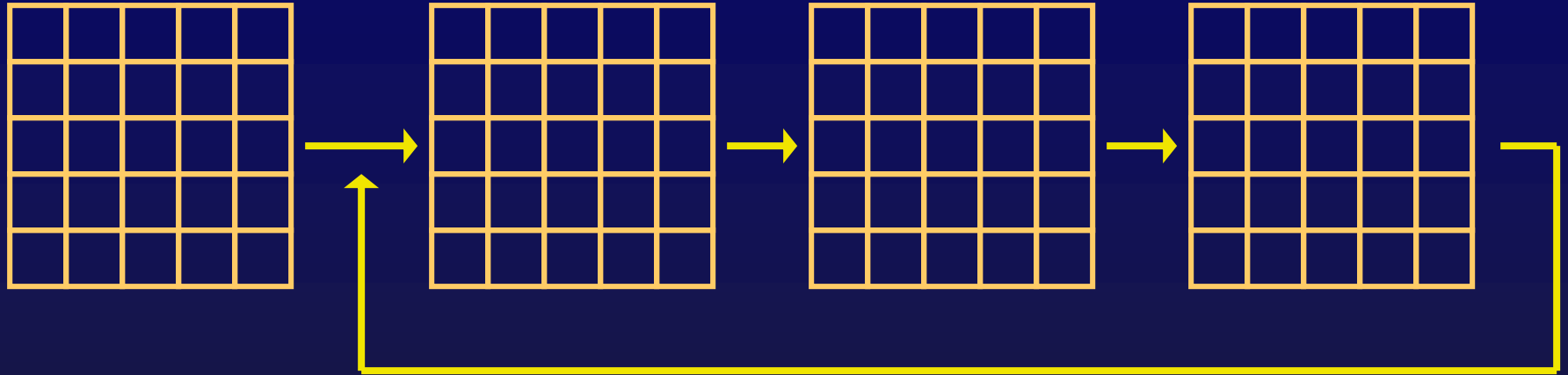
DENSITY INCREASES DUE TO SOURCES...

FLUID IN A BOX



DENSITY CONSTANT IN EACH CELL

SIMULATION



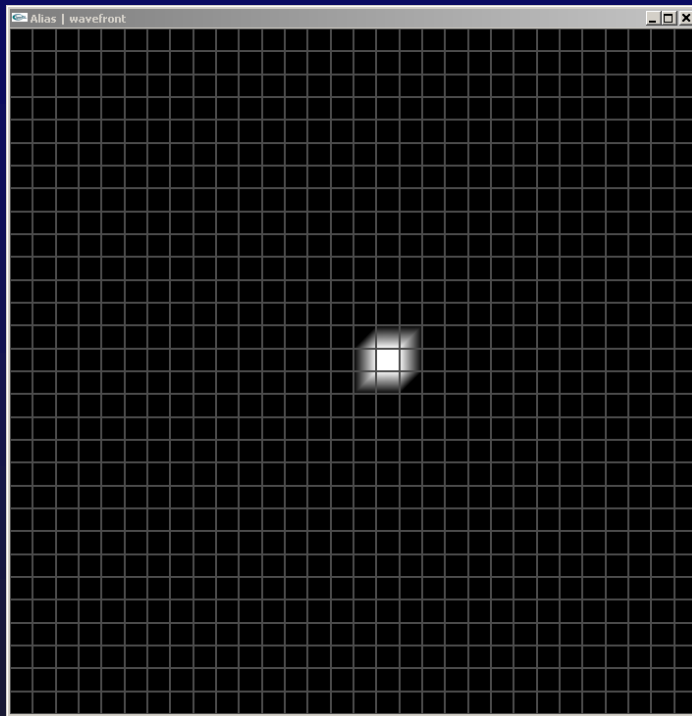
**INITIAL
STATE**

ADD SOURCES

DIFFUSE

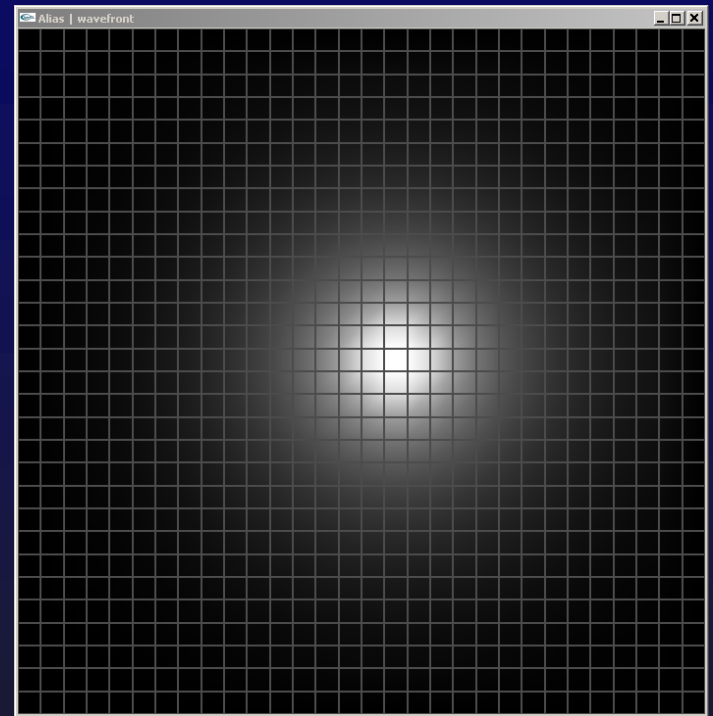
**FOLLOW
VELOCITY**

DIFFUSION STEP



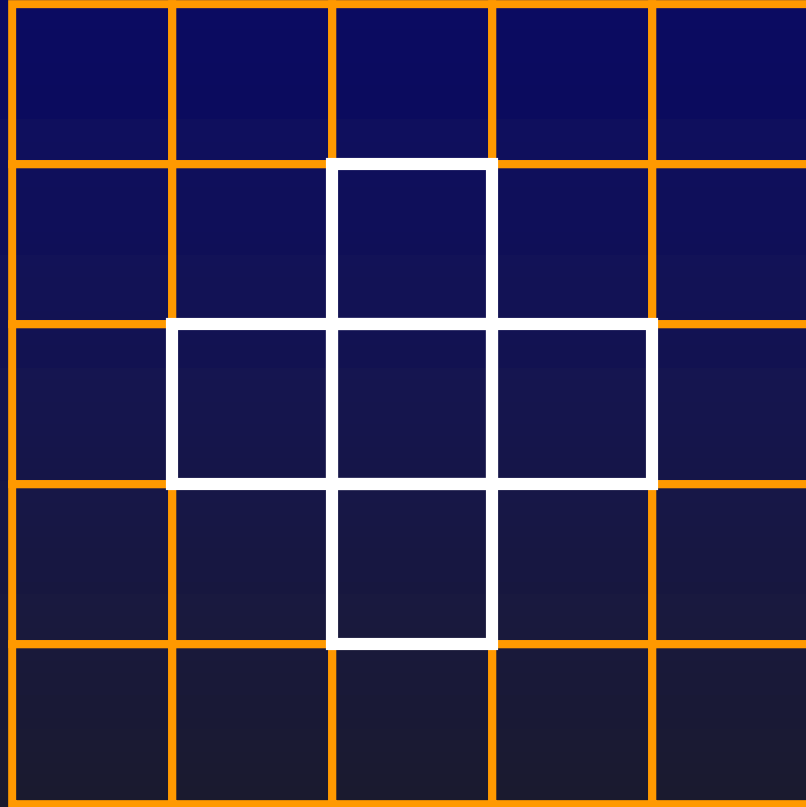
$\text{dens0}[i, j]$

→
 dt



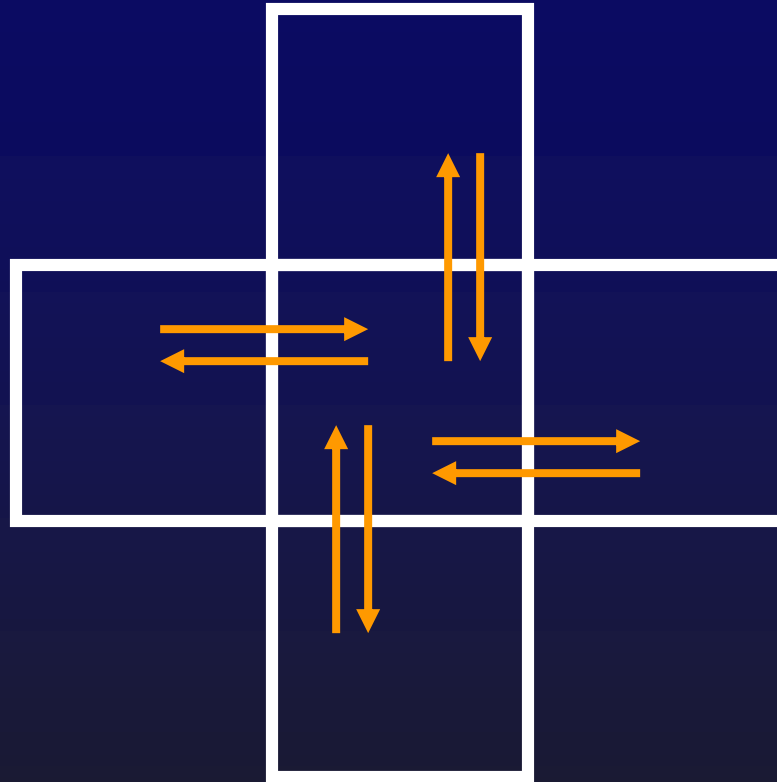
$\text{dens}[i, j]$

DIFFUSION STEP



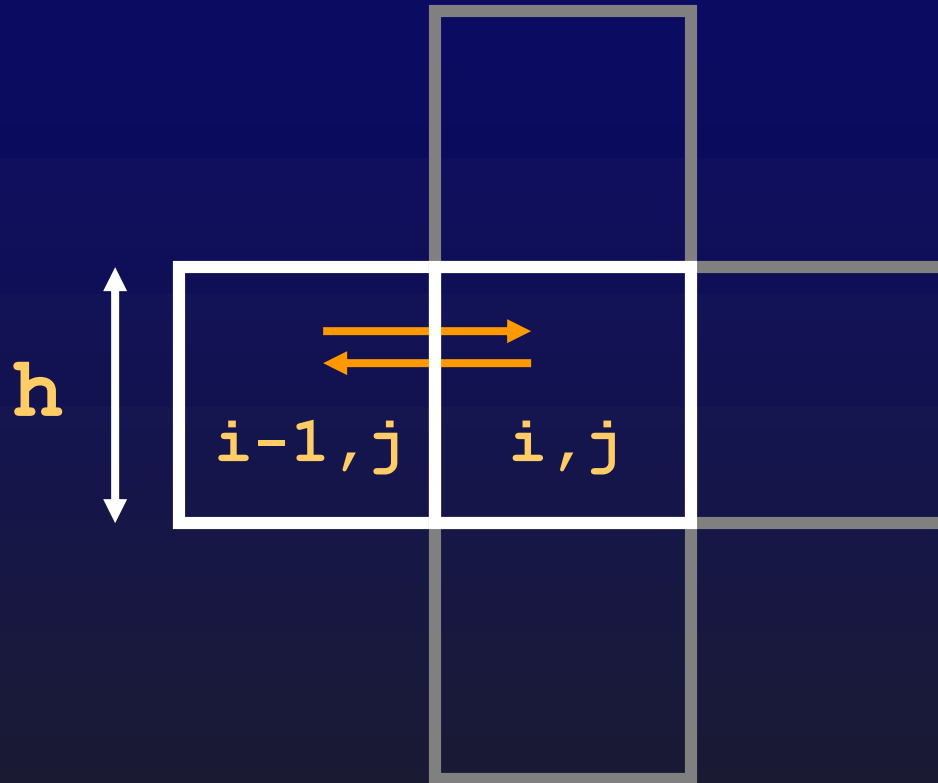
EXCHANGES BETWEEN NEIGHBORS

DIFFUSION STEP



EXCHANGES BETWEEN NEIGHBORS

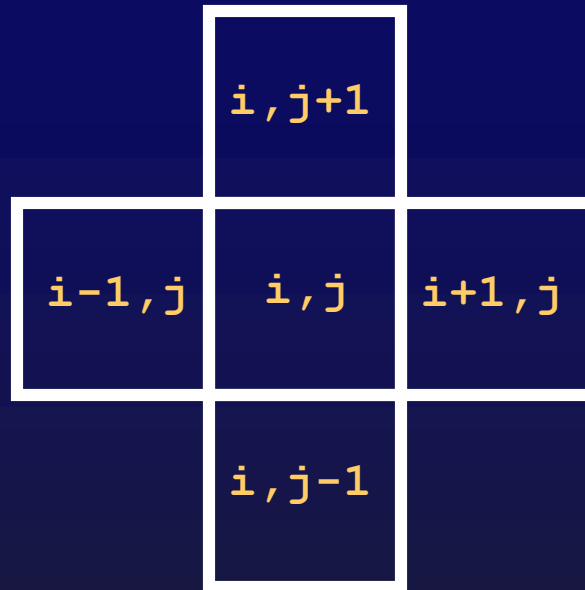
DIFFUSION STEP



CHANGE: DENSITY FLUX IN – DENSITY FLUX OUT

$$\text{diff} * dt * (\text{dens0}[i-1, j] - \text{dens0}[i, j]) / (h * h)$$

DIFFUSION STEP



```
dens[i,j] = dens0[i,j] + a*(dens0[i-1,j]+dens0[i+1,j]+  
    dens0[i,j-1]+dens0[i,j+1]-4*dens0[i,j]);
```

```
a = diff*dt/(h*h)
```

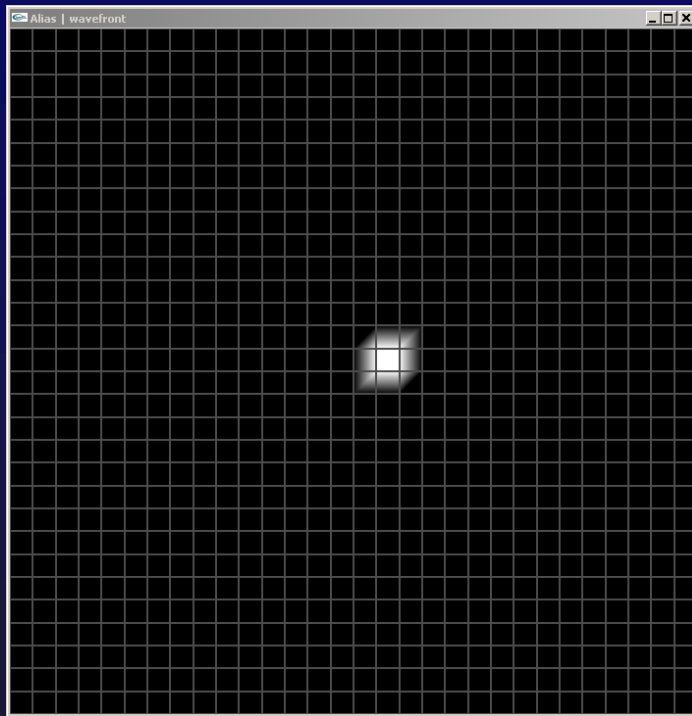
DIFFUSION STEP

```
void diffuse_bad ( float * dens, float * dens0 )
{
    int i, j;
    float a = diff*dt/(h*h);

    for ( i=1 ; i<=N ; i++ ) {
        for ( j=1 ; j<=N ; j++ ) {
            dens[i,j] = dens0[i,j] + a*(dens0[i-1,j]+dens0[i+1,j]+
                dens0[i,j-1]+dens0[i,j+1]-4*dens0[i,j]);
        }
    }
}
```

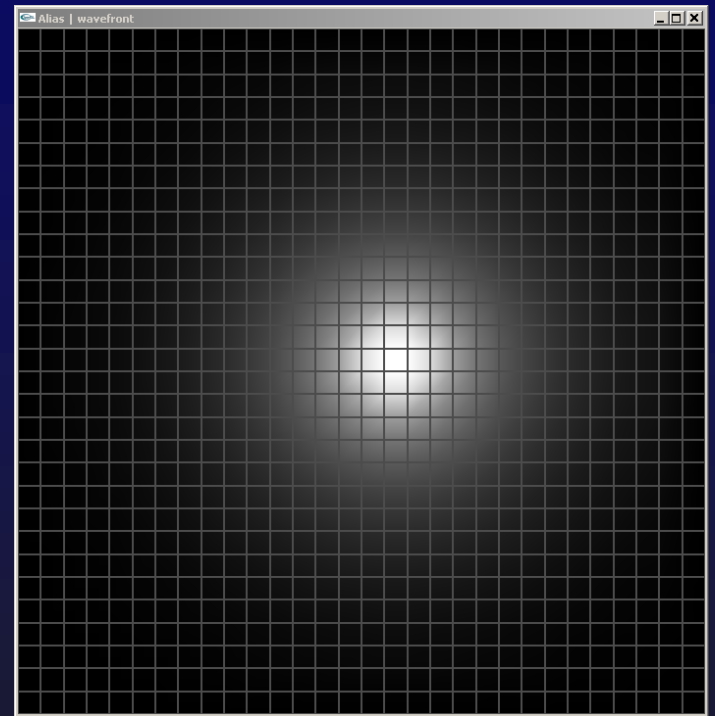
SIMPLE BUT DOESN'T WORK: UNSTABLE

DIFFUSION STEP



$\text{dens0}[i, j]$

←
-dt



$\text{dens}[i, j]$

DIFFUSE BACKWARDS: STABLE

DIFFUSION STEP

```
dens0[i,j] = dens[i,j] -  
    a*(dens[i-1,j]+dens[i+1,j]+  
        dens[i,j-1]+dens[i,j+1]-4*dens[i,j]);
```

LINEAR SYSTEM: $AX=B$

USE A FAST SPARSE SOLVER

LINEAR SOLVERS

GAUSSIAN ELIMINATION	N^3
GAUSS-SEIDEL RELAXATION	N^2
CONJUGATE GRADIENT	$N^{1.5}$
CYCLICAL REDUCTION	$N \log N$
MULTI-GRID	N

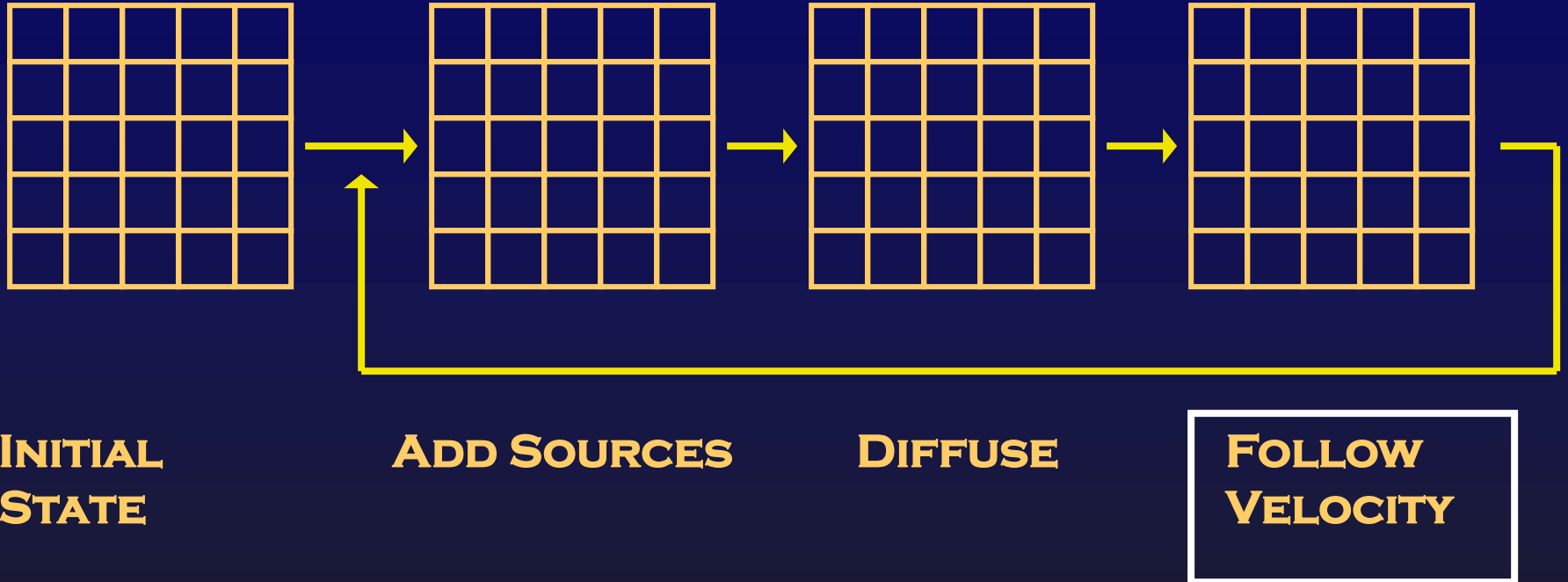
DIFFUSION STEP

```
void lin_solve ( float * x, float * b, float a, float c )
{
    int i, j, n;

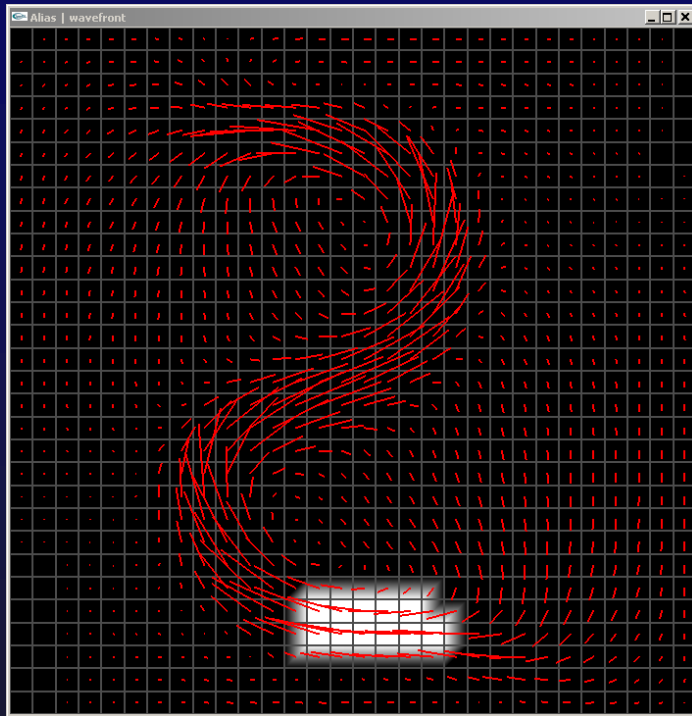
    for ( n=0 ; n<20 ; n++ ) {
        for ( i=1 ; i<=N ; i++ ) {
            for ( j=1 ; j<=N ; j++ ) {
                x[i,j] = (b[i,j] + a*(x[i-1,j]+x[i+1,j]+
                                     x[i,j-1]+x[i,j+1]))/c;
            }
        }
    }
}

void diffuse ( float * dens, float * dens0 )
{
    float a = diff*dt/(h*h);
    lin_solve ( dens, dens0, a, 1+4*a );
}
```

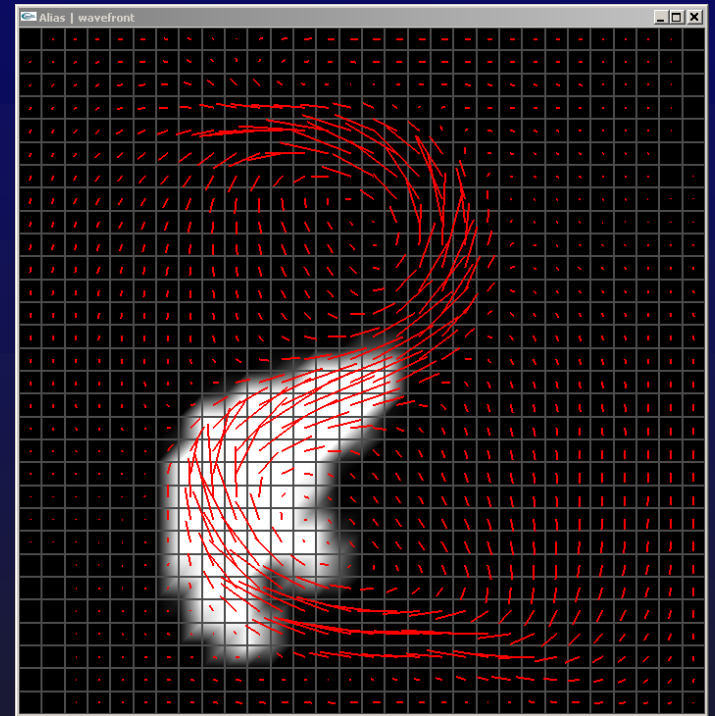

SIMULATION



FOLLOW VELOCITY



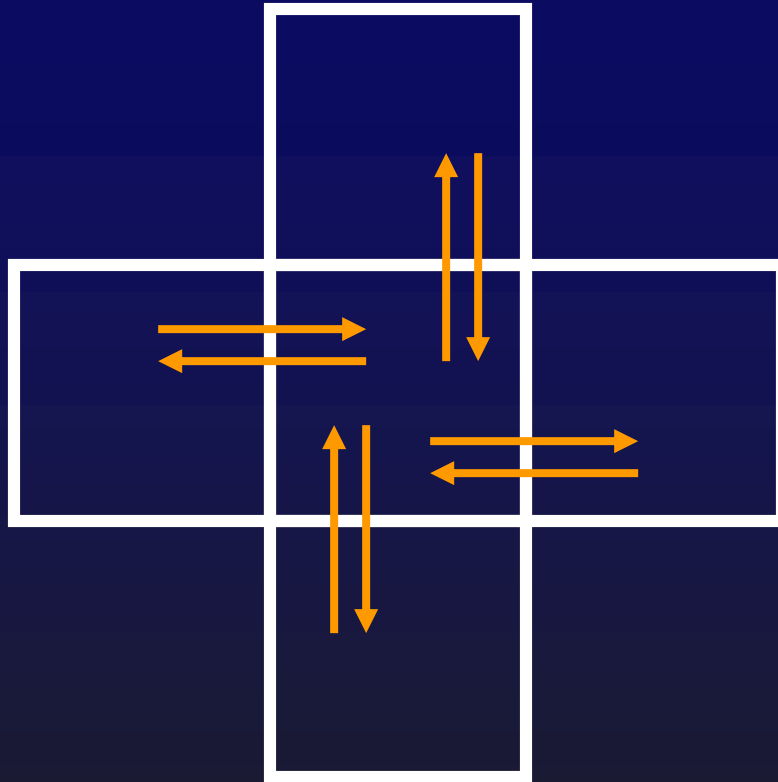
→
dt



$\text{dens0}[i, j]$
 $u[i, j], v[i, j]$

$\text{dens}[i, j]$

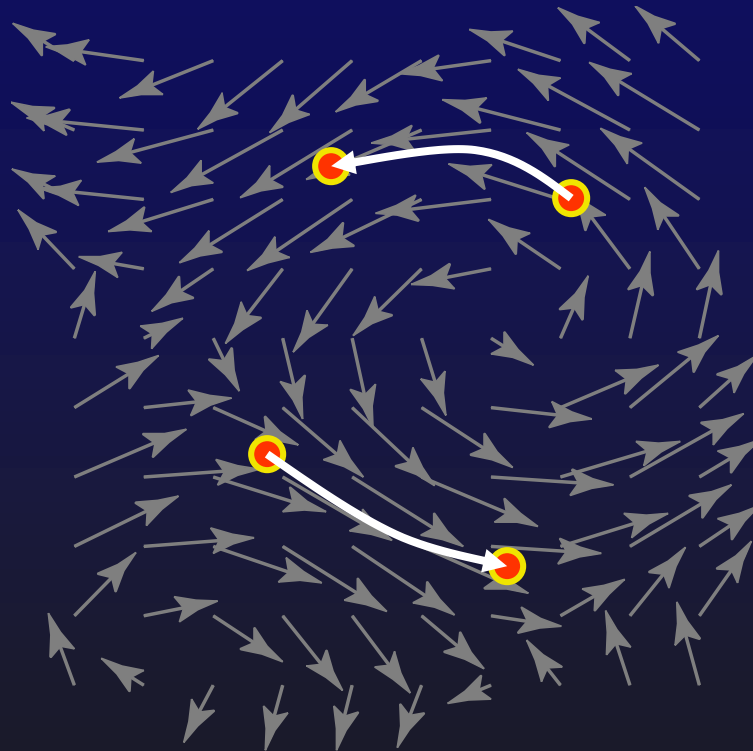
FOLLOW VELOCITY



FLUXES DEPEND ON VELOCITY

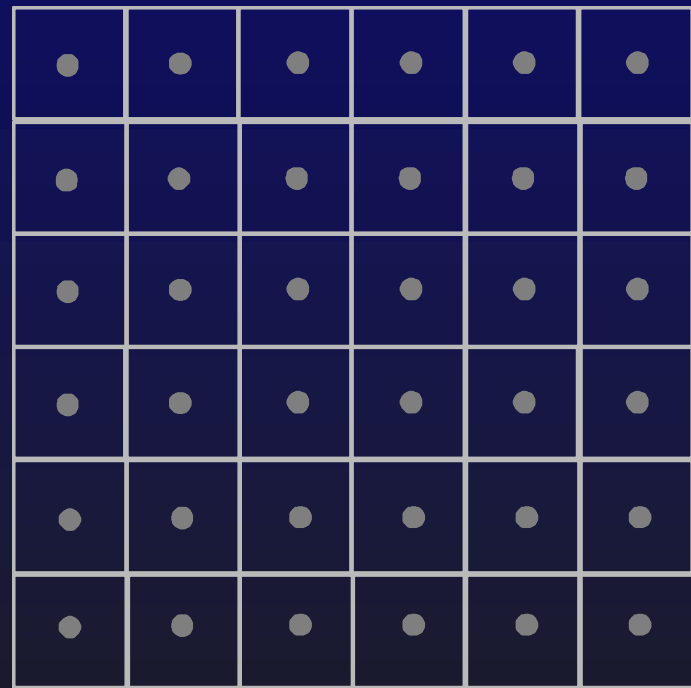
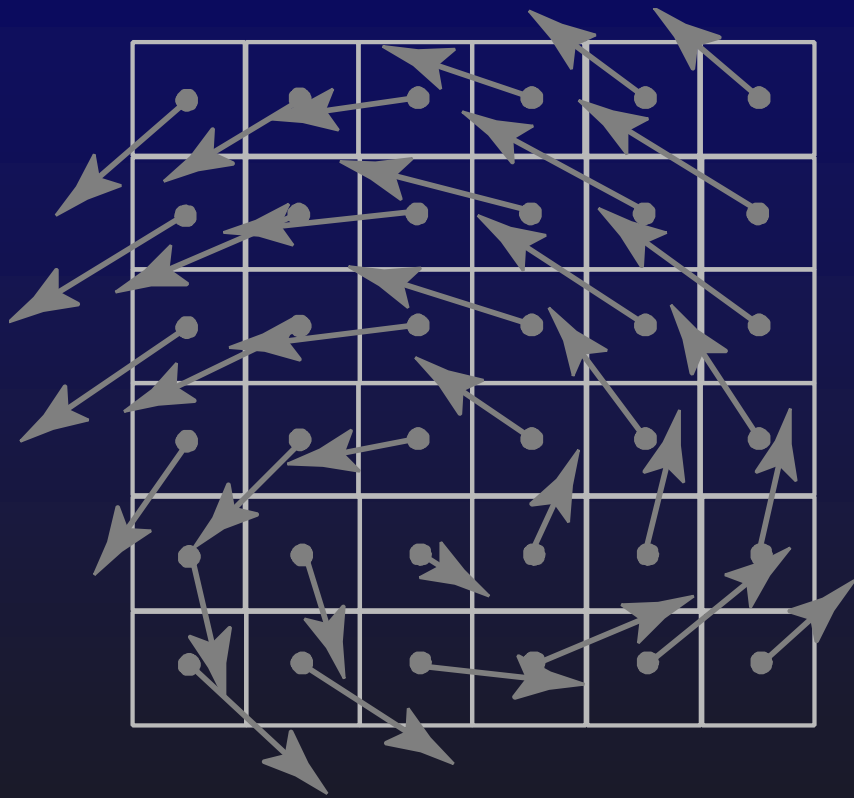
FOLLOW VELOCITY

BETTER IDEA:



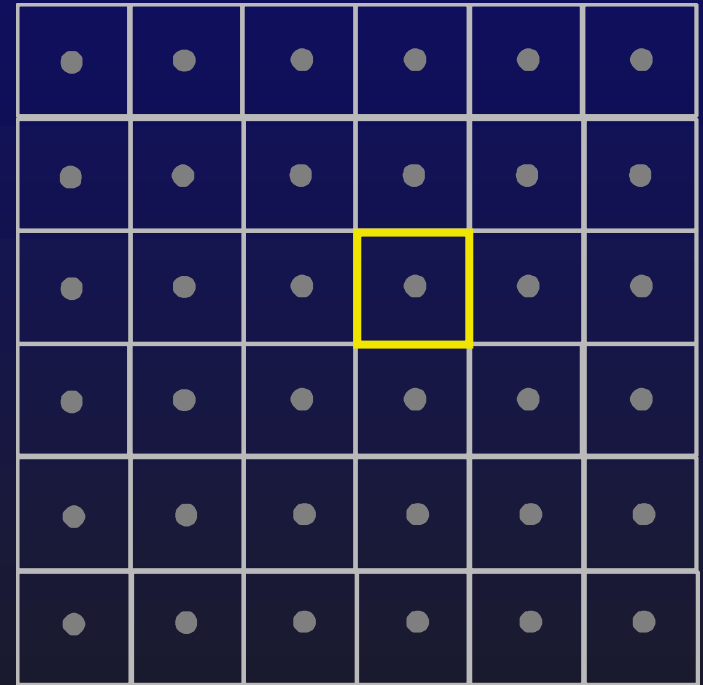
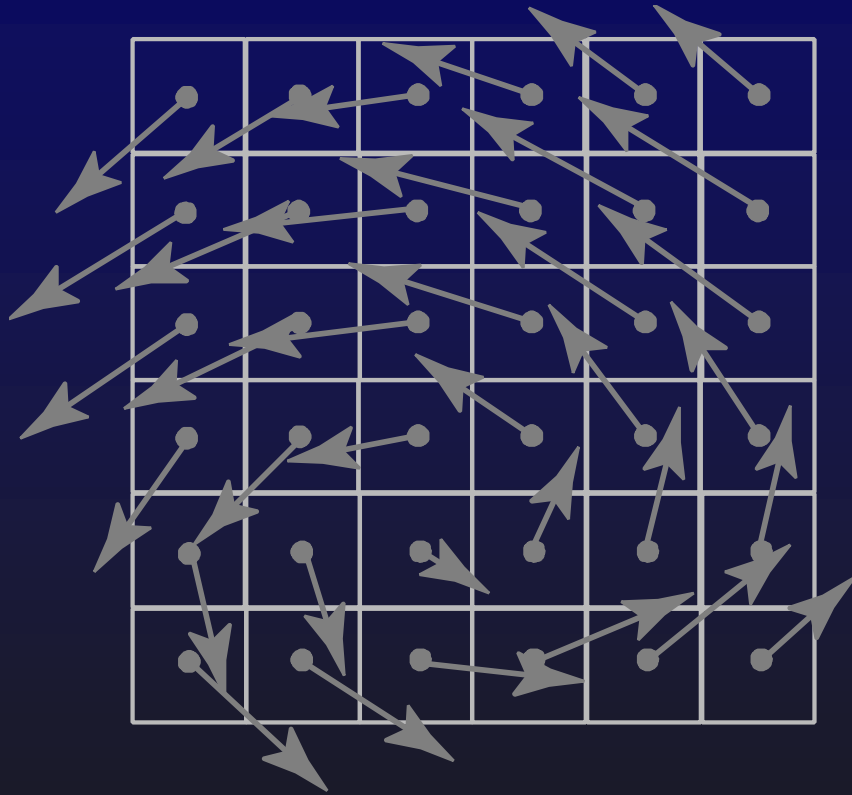
STEP EASY IF DENSITY WERE PARTICLES

FOLLOW VELOCITY



FOLLOW VELOCITY

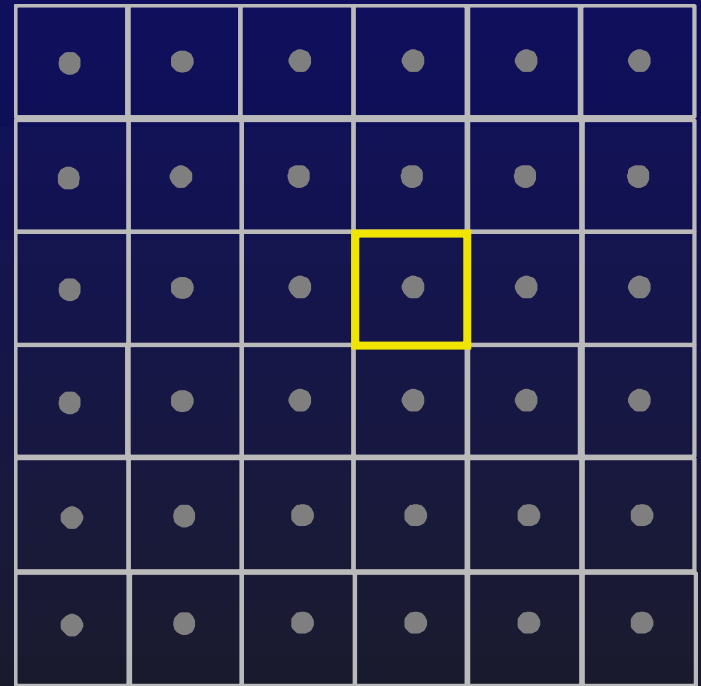
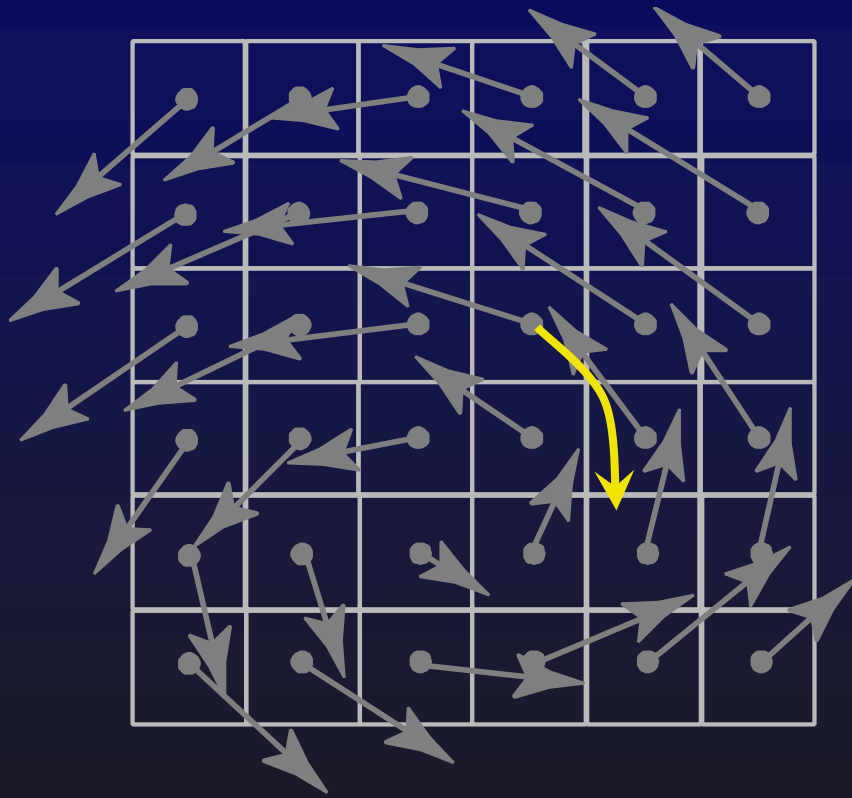
FOR EACH CELL...



`dens[i,j]`

FOLLOW VELOCITY

TRACE BACKWARD

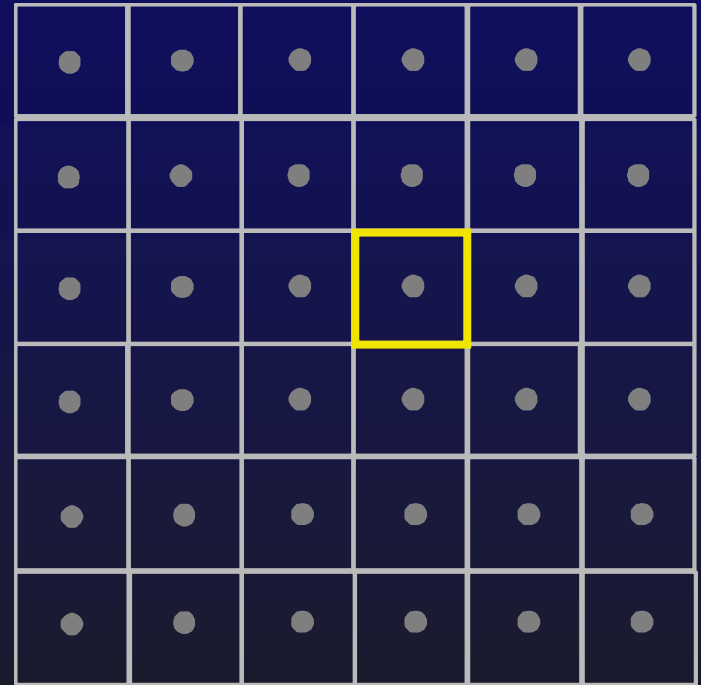
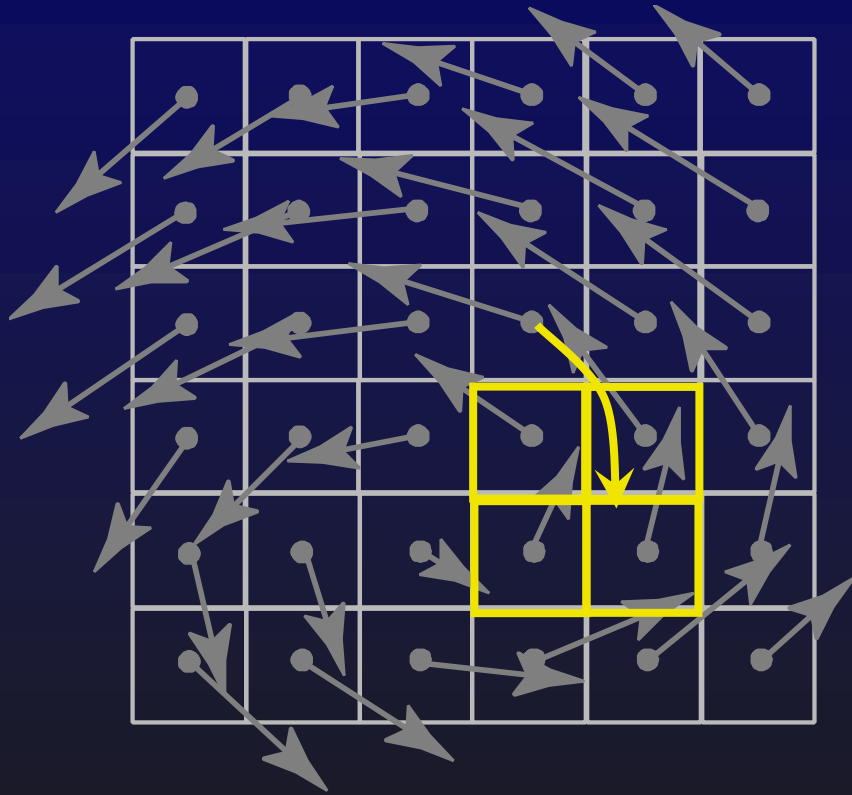


```
x = i-dt*u[i,j];
```

```
y = j-dt*v[i,j];
```

FOLLOW VELOCITY

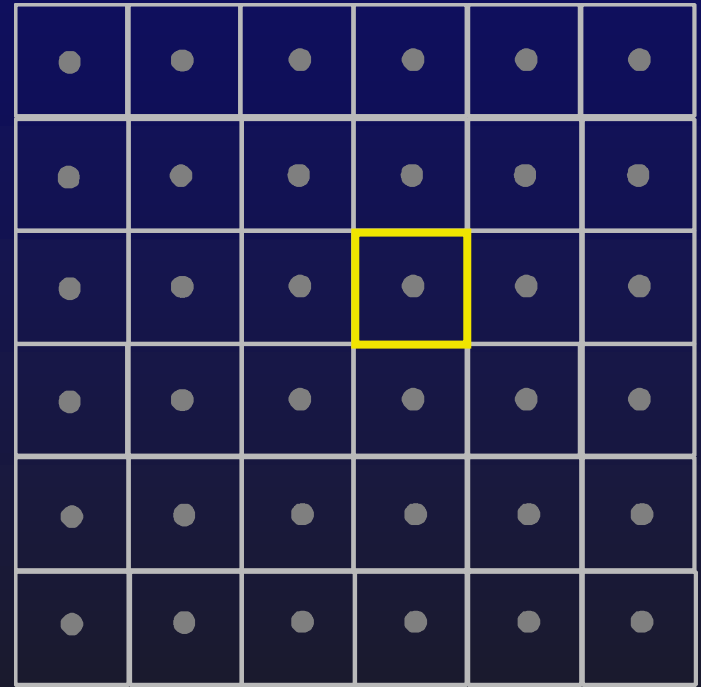
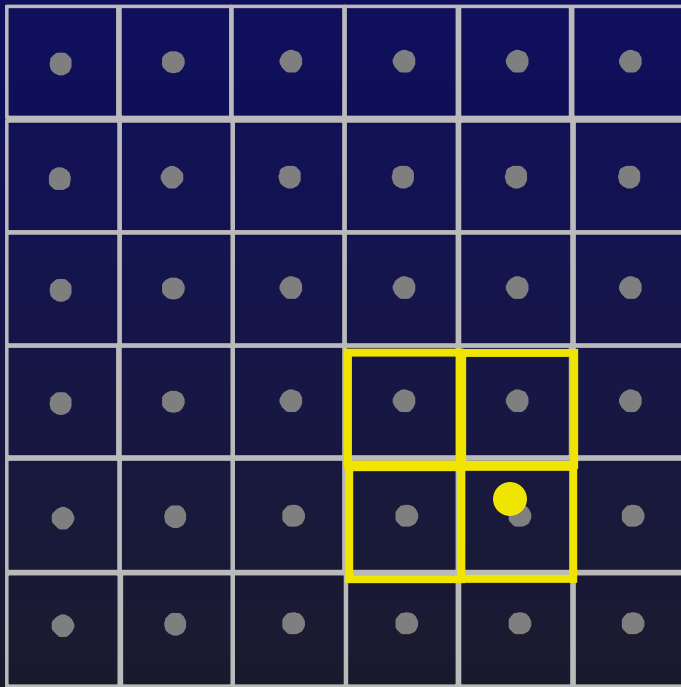
FIND FOUR NEIGHBORS



```
i0 = (int)x; i1=i0+1; s=x-i0;  
j0 = (int)y; j1=j0+1; t=y-j0;
```


FOLLOW VELOCITY

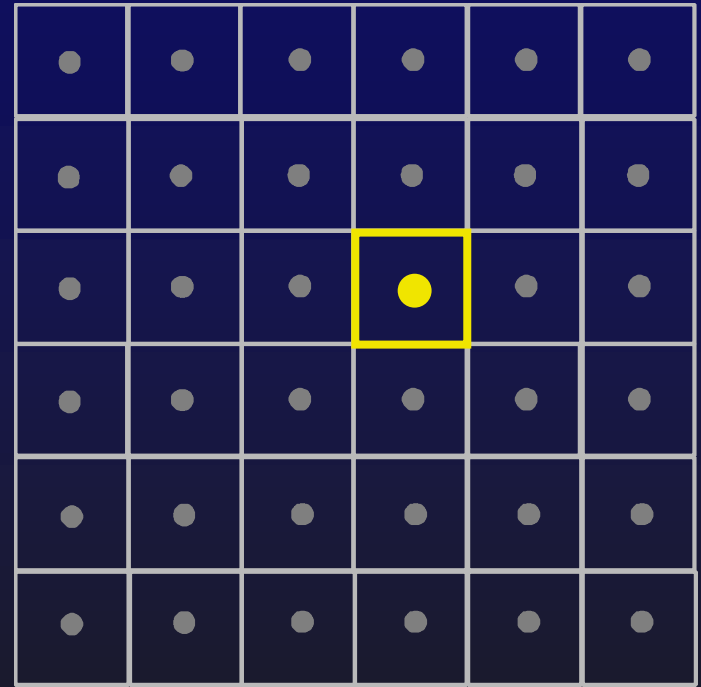
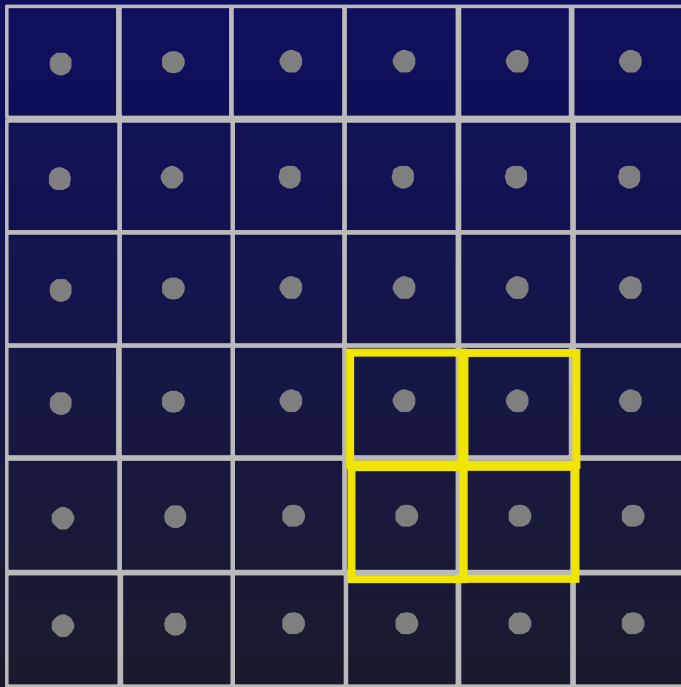
INTERPOLATE FROM NEIGHBORS



```
d = (1-s) * ((1-t)*dens0[i0,j0]+t*dens0[i0,j1]) +  
      s * ((1-t)*dens0[i1,j0]+t*dens0[i1,j1]);
```

FOLLOW VELOCITY

SET INTERPOLATED VALUE IN CELL



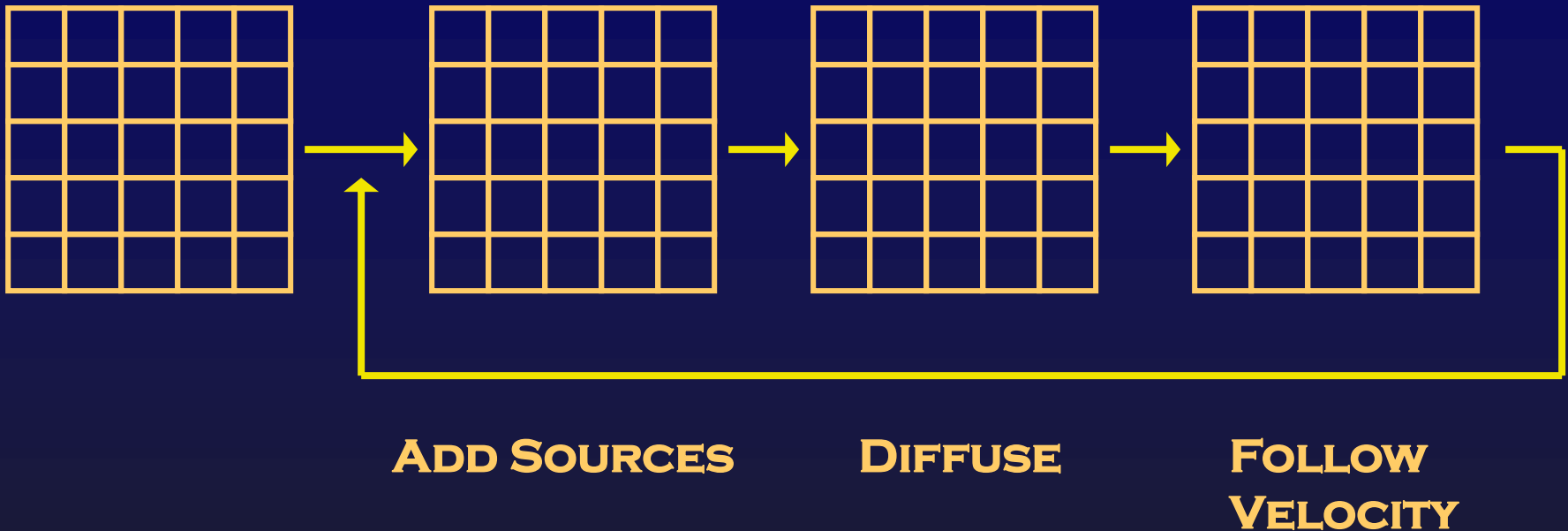
```
dens[i,j] = d;
```

FOLLOW VELOCITY

```
void advect ( float * dens, float * dens0,
float * u, float * v )
{
    int i, j, i0, j0, i1, j1;
    float x, y, s0, t0, s1, t1;

    for ( i=1 ; i<=N ; i++ ) {
        for ( j=1 ; j<=N ; j++ ) {
            x = i-dt*u[i,j]; y = j-dt*v[i,j];
            if (x<0.5) x=0.5; if (x>N+0.5) x=N+0.5;
            if (y<0.5) y=0.5; if (y>N+0.5) y=N+0.5;
            i0=(int)x; i1=i0+1; j0=(int)y; j1=j0+1;
            s1 = x-i0; s0 = 1-s1; t1 = y-j0; t0 = 1-t1;
            dens[i,j] = t0*(s0*dens0[i0,j0]+s1*dens0[i0,j1])+
                        t1*(s0*dens0[i1,j0]+s1*dens0[i1,j1]);
        }
    }
}
```

SIMULATION



```
void dens_step ()  
{  
    add_sources(dens) ;  
    SWAP(dens,dens0) ; diffuse(dens,dens0) ;  
    SWAP(dens,dens0) ; advect(dens,dens0,u,v) ;  
}
```

NAVIER-STOKES EQUATIONS

$$\frac{\partial \mathbf{u}}{\partial t} = -(\mathbf{u} \cdot \nabla) \mathbf{u} + \nu \nabla^2 \mathbf{u} + \mathbf{f}$$

VELOCITY

$$\frac{\partial \rho}{\partial t} = -(\mathbf{u} \cdot \nabla) \rho + \kappa \nabla^2 \rho + S$$

DENSITY

VELOCITY SOLVER

```
void velocity_step ()
{
    add_sources(u);
    add_sources(v);
    SWAP(u,u0); SWAP(v,v0);
    diffuse(u,u0);
    diffuse(v,v0);
    SWAP(u,u0); SWAP(v,v0);
    advect(u,u0,u0,v0);
    advect(v,v0,u0,v0);
    project(u,v,u0,v0);
}
```

```
void dens_step ()
{
    add_sources(dens);

    SWAP(dens,dens0);
    diffuse(dens,dens0);

    SWAP(dens,dens0);
    advect(dens,dens0,u,v);
}
```

**REUSE DENSITY SOLVER CODE
EXCEPT FOR ONE ROUTINE...**

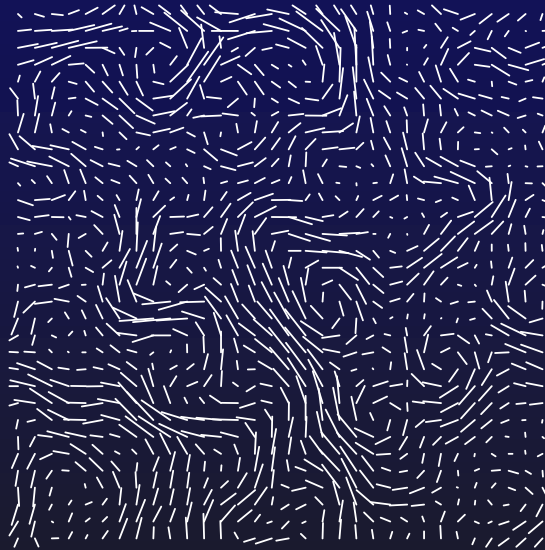
PROJECTION STEP

HODGE DECOMPOSITION:



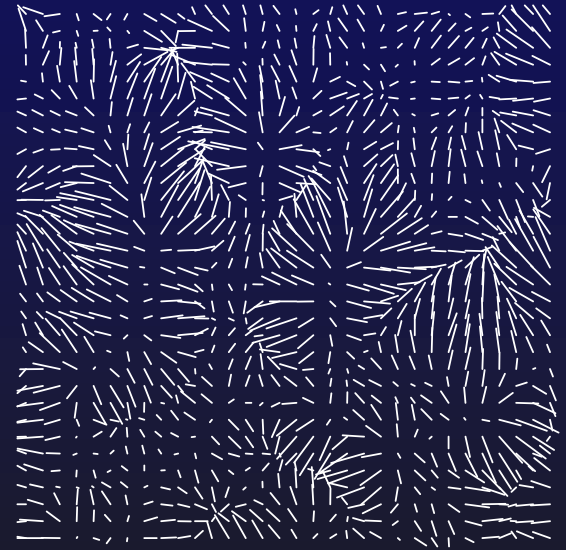
ANY FIELD

=



MASS CONSERVING

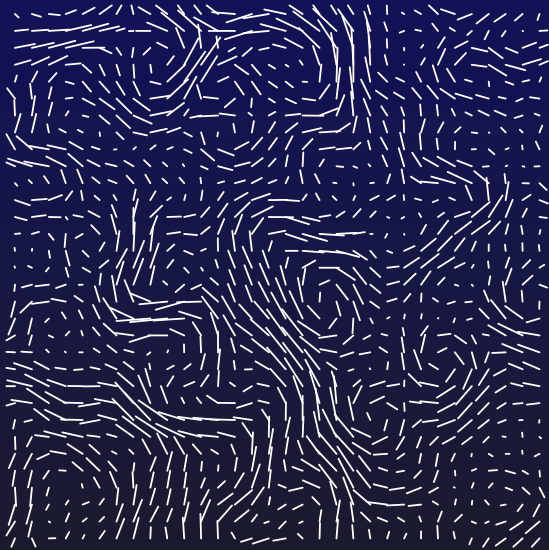
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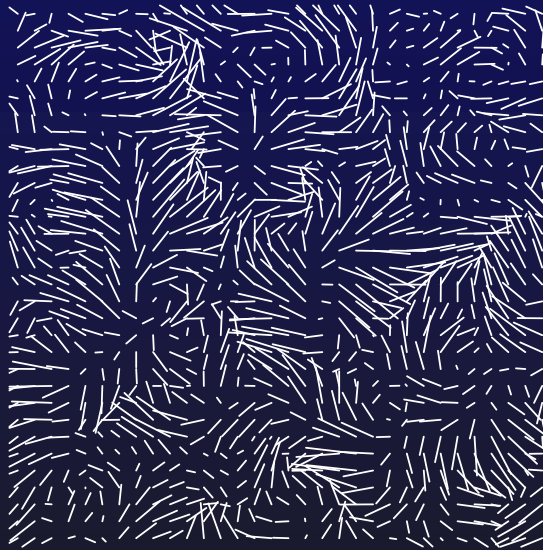
GRADIENT

PROJECTION STEP

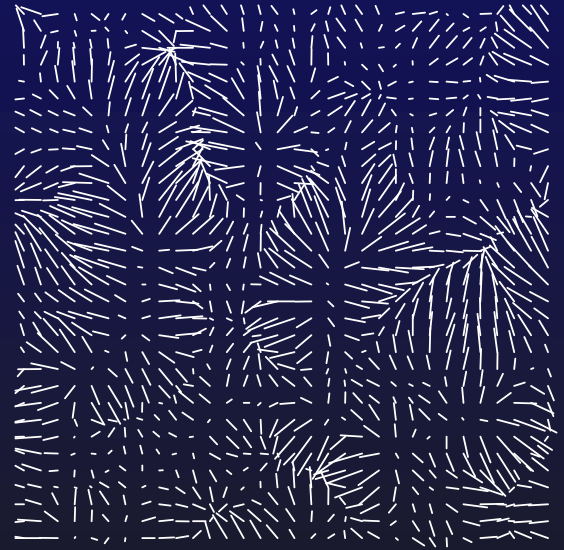
SUBTRACT GRADIENT FIELD



$=$



$-$



MASS CONSERVING

ANY FIELD

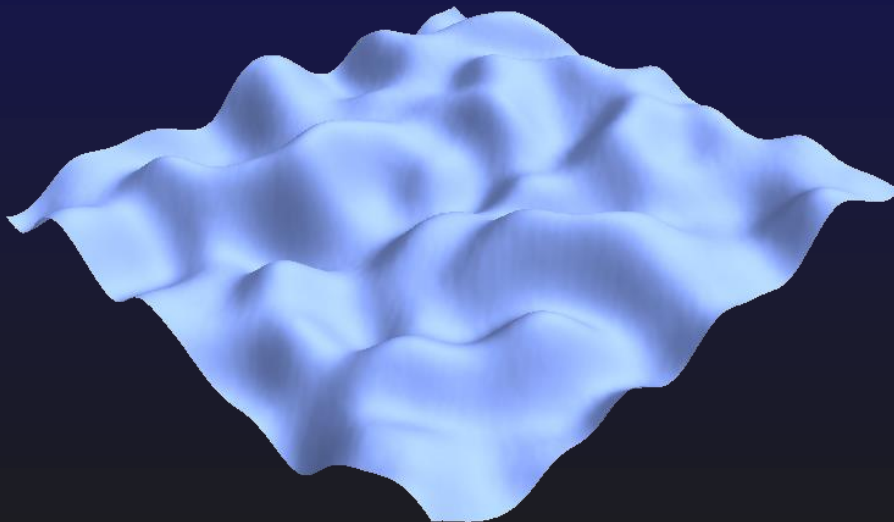
GRADIENT

PROJECTION STEP

**GRADIENT: DIRECTION OF STEEPEST DESCENT OF
A HEIGHT FIELD.**

$$G_x[i,j] = 0.5 * (p[i+1,j] - p[i-1,j]) / h$$

$$G_y[i,j] = 0.5 * (p[i,j+1] - p[i,j-1]) / h$$



$p[i,j]$

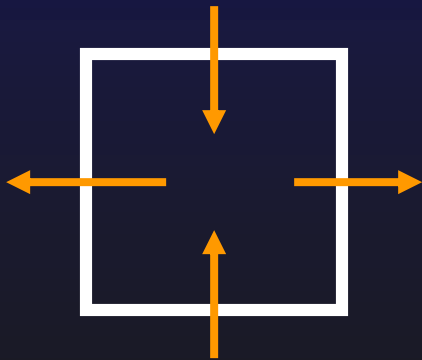
PROJECTION STEP

HEIGHT FIELD SATISFIES A POISSON EQUATION

$$4*p[i,j]-p[i+1,j]+p[i-1,j]+p[i,j+1]+p[i,j-1] = \text{div}[i,j]$$

$$\text{div}[i,j] = -0.5*h*(u[i+1,j]-u[i-1,j]+v[i,j+1]-v[i,j-1])$$

IDEALLY DIV IS ZERO: FLOW IN = FLOW OUT



REUSE LINEAR SOLVER OF THE DIFFUSION STEP

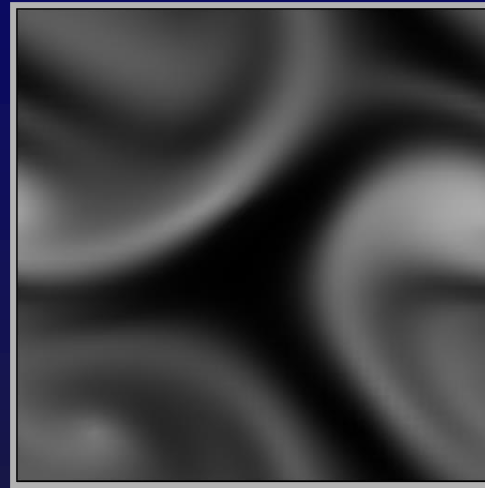
PROJECTION STEP

```
void project ( float * u, float * v, float * div, float * p )
{
    int i, j;
    // compute divergence
    for ( i=1 ; i<=N ; i++ ) {
        for ( j=1 ; j<=N ; j++ ) {
            div[i,j] = -0.5*h*(u[i+1,j]-u[i-1,j]+v[i,j+1]-v[i,j-1]);
            p[i,j] = 0.0;
        }
    }
    set_bnd ( 0, div ); set_bnd ( 0, p );
    // solve Poisson equation
    lin_solve ( p, div, 1, 4 );
    // subtract gradient field
    for ( i=1 ; i<=N ; i++ ) {
        for ( j=1 ; j<=N ; j++ ) {
            u[i,j] -= 0.5*(p[i+1,j]-p[i-1,j])/h;
            v[i,j] -= 0.5*(p[i,j+1]-p[i,j-1])/h;
        }
    }
}
```

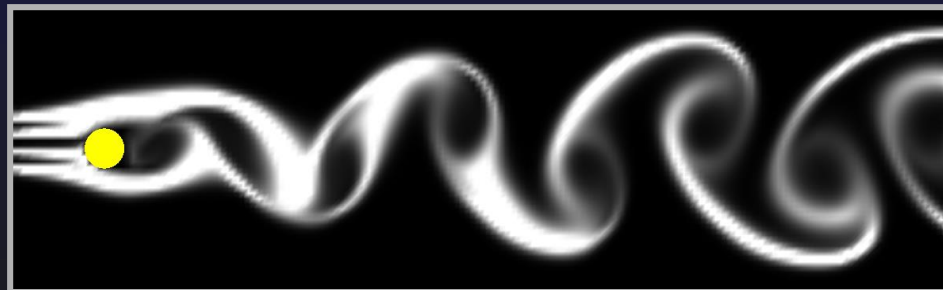
BOUNDARIES



FIXED WALLS

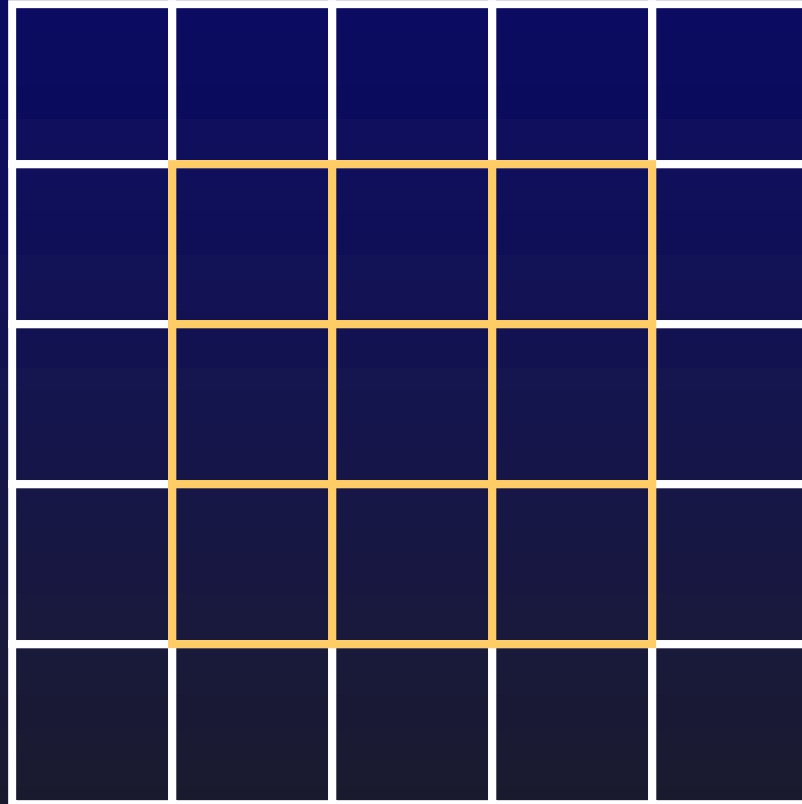


PERIODIC



INFLOW + INTERNAL

BOUNDARIES



ADD ANOTHER LAYER AROUND THE GRID

BOUNDARIES

	0.5	0.1	0.2	
	0.4	0.2	0.0	
	0.2	0.1	0.0	

DENSITIES: SIMPLY COPY OVER VALUES

BOUNDARIES

0.0	0.5	0.1	0.2	0.0
-0.5	0.5	0.1	0.2	-0.2
-0.4	0.4	0.2	0.0	-0.0
-0.2	0.2	0.1	0.0	-0.0
0.0	0.2	0.1	0.0	0.0

U-VELOCITY: ZERO ON VERTICAL BOUNDARIES

BOUNDARIES

0.0	-0.5	-0.1	-0.2	0.0
0.5	0.5	0.1	0.2	0.2
0.4	0.4	0.2	0.0	0.0
0.2	0.2	0.1	0.0	0.0
0.0	-0.2	-0.1	-0.0	0.0

V-VELOCITY: ZERO ON HORIZONTAL BOUNDARIES

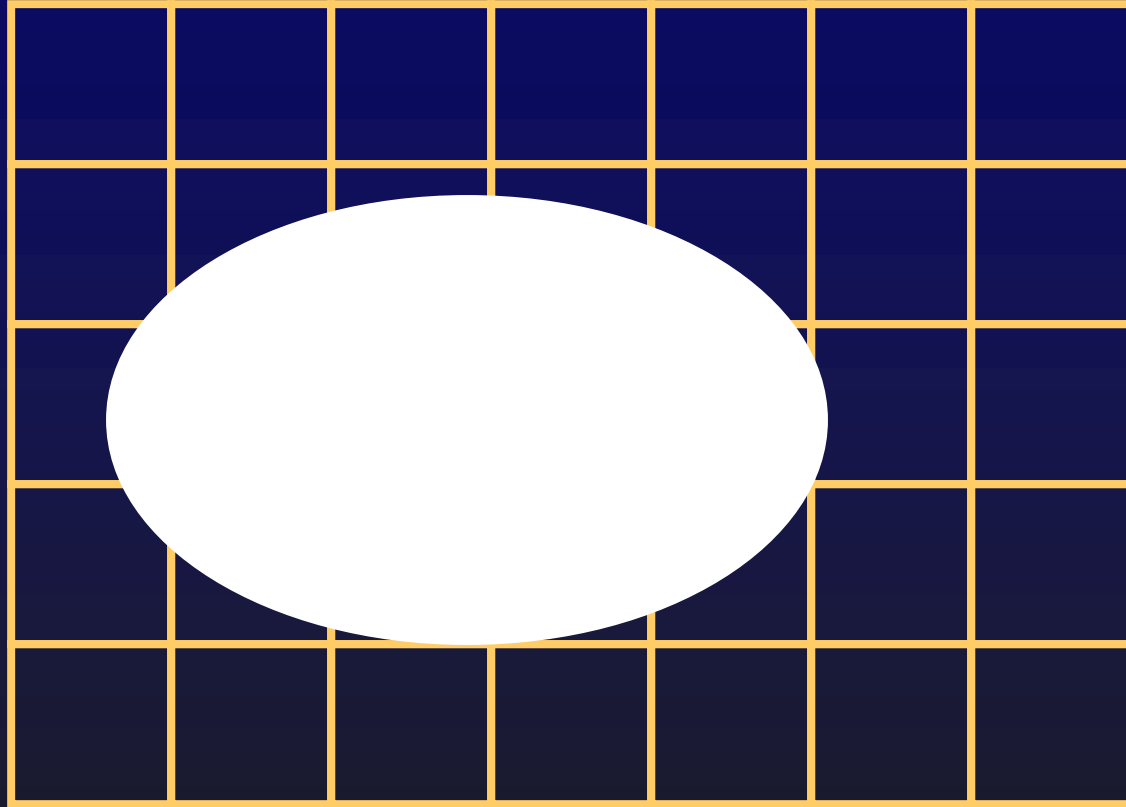
BOUNDARIES

```
void set_bnd ( int b, float * x )
{
    int i;

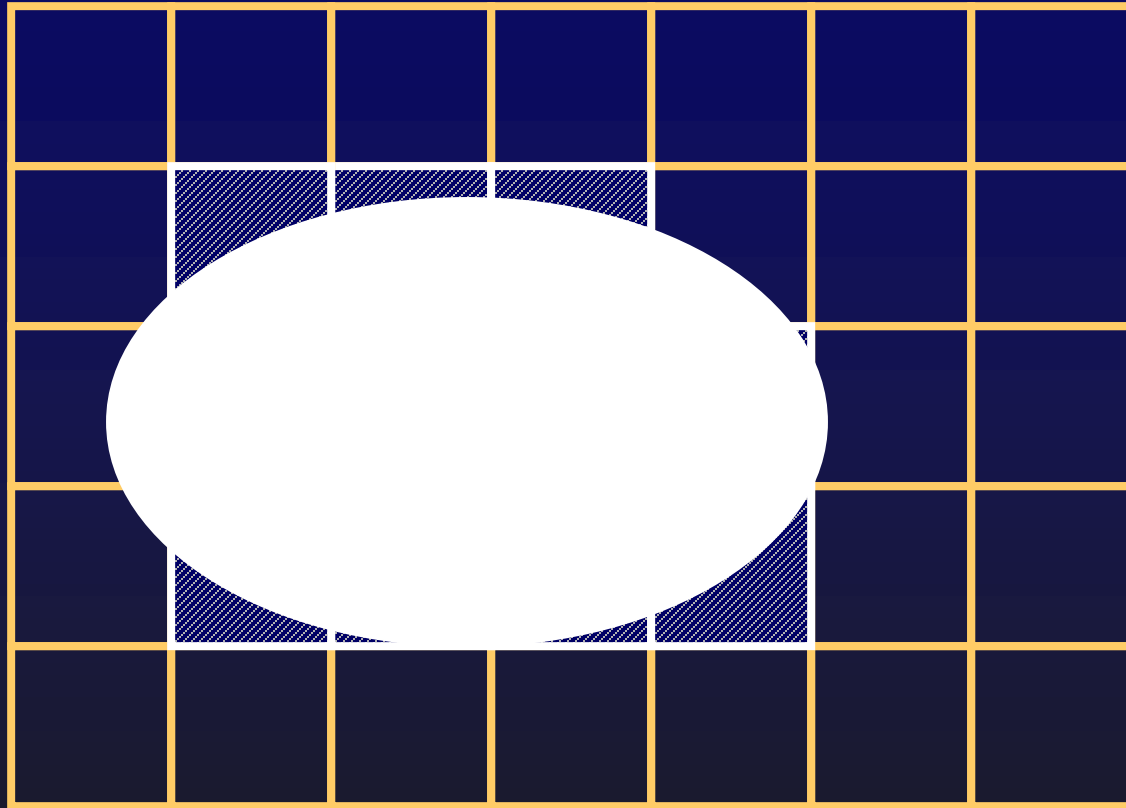
    for ( i=1 ; i<=N ; i++ ) {
        x[0 ,i ] = b==1 ? -x[1,i] : x[1,i];
        x[N+1,i ] = b==1 ? -x[N,i] : x[N,i];
        x[i ,0 ] = b==2 ? -x[i,1] : x[i,1];
        x[i ,N+1] = b==2 ? -x[i,N] : x[i,N];
    }
    x[0 ,0 ] = 0.5*(x[1,0 ]+x[0 ,1]);
    x[0 ,N+1] = 0.5*(x[1,N+1]+x[0 ,N]);
    x[N+1,0 ] = 0.5*(x[N,0 ]+x[N+1,1]);
    x[N+1,N+1] = 0.5*(x[N,N+1]+x[N+1,N]);
}
```

CALL AFTER EVERY UPDATE OF THE GRIDS

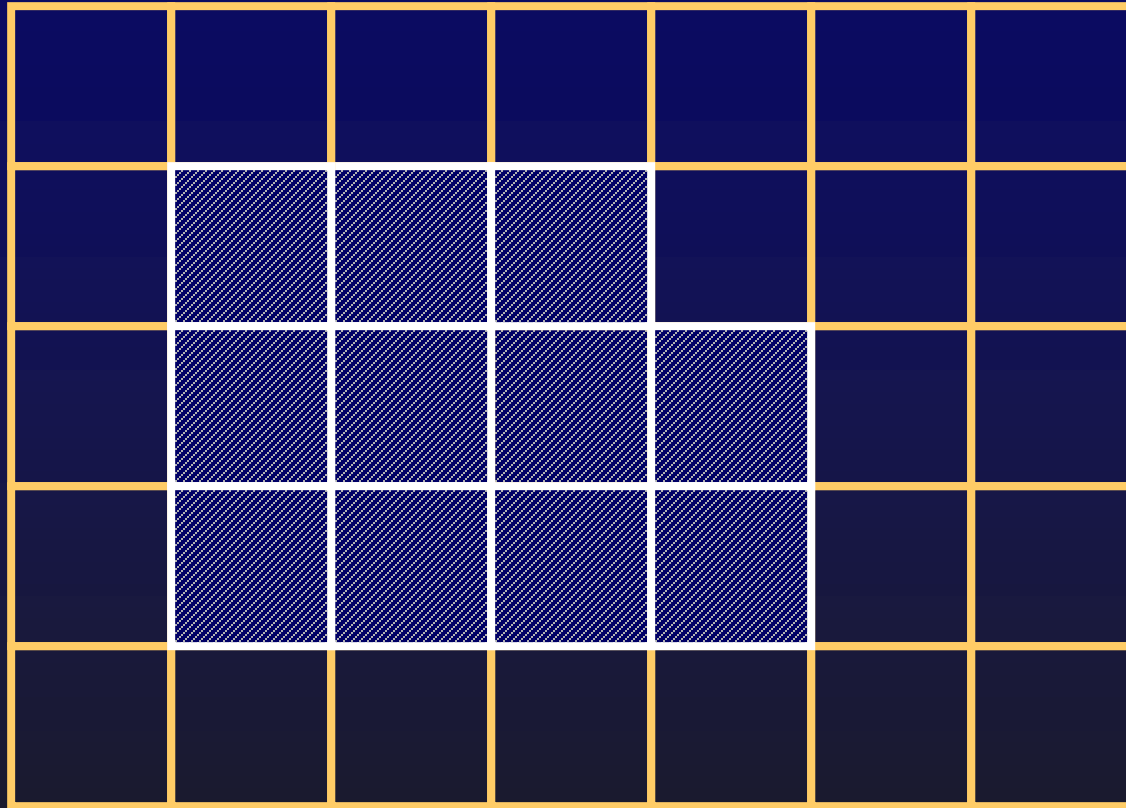
INTERNAL BOUNDARIES



INTERNAL BOUNDARIES



INTERNAL BOUNDARIES



INTERNAL BOUNDARIES

0.0	0.0	0.5	0.1	0.2	0.1	0.3
0.4				0.3	0.2	0.5
0.6					0.5	0.6
0.5					0.8	0.7
0.5	0.1	0.2	0.1	0.2	0.7	0.9

FOR DENSITY

INTERNAL BOUNDARIES

0.0	0.0	0.5	0.1	0.2	0.1	0.3
0.4	0.2	0.5	0.2	0.3	0.2	0.5
0.6	0.6	0.0	0.0	0.4	0.5	0.6
0.5	0.2	0.2	0.1	0.5	0.8	0.7
0.5	0.1	0.2	0.1	0.2	0.7	0.9

FOR DENSITY

THE CODE

**ENTIRE SOLVER IN 100 LINES OF
(READABLE) C-CODE...**

```

#define IX(i,j) ((i)+(N+2)*(j))
#define SWAP(x0,x) {float * tmp=x0;x0=x;x=tmp;}
#define FOR_EACH_CELL for ( i=1 ; i<=N ; i++ ) {\
                                for ( j=1 ; j<=N ; j++ ) {
#define END_FOR }}

void add_source(int N, float *x, float *s, float dt)
{
    int i, size=(N+2)*(N+2);
    for ( i=0 ; i<size ; i++ ) x[i] += dt*s[i];
}

void set_bnd(int N, int b, float *x)
{
    int i;

    for ( i=1 ; i<=N ; i++ ) {
        x[IX(0 ,i)] = b==1 ? -x[IX(1,i)] : x[IX(1,i)];
        x[IX(N+1,i)] = b==1 ? -x[IX(N,i)] : x[IX(N,i)];
        x[IX(i,0 )] = b==2 ? -x[IX(i,1)] : x[IX(i,1)];
        x[IX(i,N+1)] = b==2 ? -x[IX(i,N)] : x[IX(i,N)];
    }
    x[IX(0 ,0 )] = 0.5f*(x[IX(1,0 )]+x[IX(0 ,1)]);
    x[IX(0 ,N+1)] = 0.5f*(x[IX(1,N+1)]+x[IX(0 ,N)]);
    x[IX(N+1,0 )] = 0.5f*(x[IX(N,0 )]+x[IX(N+1,1)]);
    x[IX(N+1,N+1)] = 0.5f*(x[IX(N,N+1)]+x[IX(N+1,N)]);
}

void lin_solve(int N, int b, float *x, float *x0,
float a, float c)
{
    int i, j, n;

    for ( n=0 ; n<20 ; n++ ) {
        FOR_EACH_CELL
            x[IX(i,j)] = (x0[IX(i,j)]+a*(x[IX(i-1,j)]+
                x[IX(i+1,j)]+x[IX(i,j-1)]+x[IX(i,j+1)]))/c;
        END_FOR
        set_bnd ( N, b, x );
    }
}

void diffuse(int N, int b, float *x, float *x0,
float diff, float dt)
{
    float a=dt*diff*N*N;
    lin_solve ( N, b, x, x0, a, 1+4*a );
}

```

```

void advect(int N, int b, float *d, float *d0, float *u, float *v, float dt)
{
    int i, j, i0, j0, i1, j1;
    float x, y, s0, t0, s1, t1, dt0;

    dt0 = dt*N;
    FOR_EACH_CELL
        x = i-dt0*u[IX(i,j)]; y = j-dt0*v[IX(i,j)];
        if (x<0.5f) x=0.5f; if (x>N+0.5f) x=N+0.5f; i0=(int)x; i1=i0+1;
        if (y<0.5f) y=0.5f; if (y>N+0.5f) y=N+0.5f; j0=(int)y; j1=j0+1;
        s1 = x-i0; s0 = 1-s1; t1 = y-j0; t0 = 1-t1;
        d[IX(i,j)] = s0*(t0*d0[IX(i0,j0)]+t1*d0[IX(i0,j1)])+
            s1*(t0*d0[IX(i1,j0)]+t1*d0[IX(i1,j1)]);
    END_FOR
    set_bnd ( N, b, d );
}

void project(int N, float * u, float * v, float * p, float * div)
{
    int i, j;

    FOR_EACH_CELL
        div[IX(i,j)] = -0.5f*(u[IX(i+1,j)]-u[IX(i-1,j)]+v[IX(i,j+1)]-v[IX(i,j-1)])/N;
        p[IX(i,j)] = 0;
    END_FOR
    set_bnd ( N, 0, div ); set_bnd ( N, 0, p );

    lin_solve ( N, 0, p, div, 1, 4 );

    FOR_EACH_CELL
        u[IX(i,j)] -= 0.5f*N*(p[IX(i+1,j)]-p[IX(i-1,j)]);
        v[IX(i,j)] -= 0.5f*N*(p[IX(i,j+1)]-p[IX(i,j-1)]);
    END_FOR
    set_bnd ( N, 1, u ); set_bnd ( N, 2, v );
}

void dens_step(int N, float *x, float *x0, float *u, float *v, float diff, float dt)
{
    add_source ( N, x, x0, dt );
    SWAP ( x0, x ); diffuse ( N, 0, x, x0, diff, dt );
    SWAP ( x0, x ); advect ( N, 0, x, x0, u, v, dt );
}

void vel_step(int N, float *u, float *v, float *u0, float *v0, float visc, float dt)
{
    add_source ( N, u, u0, dt ); add_source ( N, v, v0, dt );
    SWAP ( u0, u ); diffuse ( N, 1, u, u0, visc, dt );
    SWAP ( v0, v ); diffuse ( N, 2, v, v0, visc, dt );
    project ( N, u, v, u0, v0 );
    SWAP ( u0, u ); SWAP ( v0, v );
    advect ( N, 1, u, u0, u0, v0, dt ); advect ( N, 2, v, v0, u0, v0, dt );
    project ( N, u, v, u0, v0 );
}

```


GUIDE TO THE LITERATURE

(COMPUTATIONAL FLUID DYNAMICS)

DIFFUSION STEP ⇐ IMPLICIT METHODS

- ANY STANDARD TEXT IN NUMERICAL METHODS

ADVECTION STEP ⇐ SEMI-LAGRANGIAN

- COURANT ET AL., *COMM. PURE & APP. MATH.*, 1952.
- WEATHER FORECASTING
- REDISCOVERED MANY TIMES...

PROJECTION STEP ⇐ PROJECTION METHODS

- CHORIN, *MATH. COMPUT.*, 1969.

GUIDE TO THE LITERATURE

(COMPUTER GRAPHICS)

VORTEX BLOB — RESTRICTED TO 2D

- UPSON & YAEGER, PROC. *SIGGRAPH*, 1986.
- GAMITO ET AL., *EUROGRAPHICS*, 1995.

EXPLICIT FINITE DIFFERENCES → UNSTABLE

- FOSTER & METAXAS, *GMIP*, 1996.
- FOSTER & METAXAS, PROC. *SIGGRAPH*, 1997.
- CHEN ET AL., *IEEE CG&A*, 1997.

IMPLICIT—SEMI-LAGRANGIAN → STABLE

- STAM, PROC. *SIGGRAPH*, 1999.

FEDKIW'S GROUP AT STANFORD

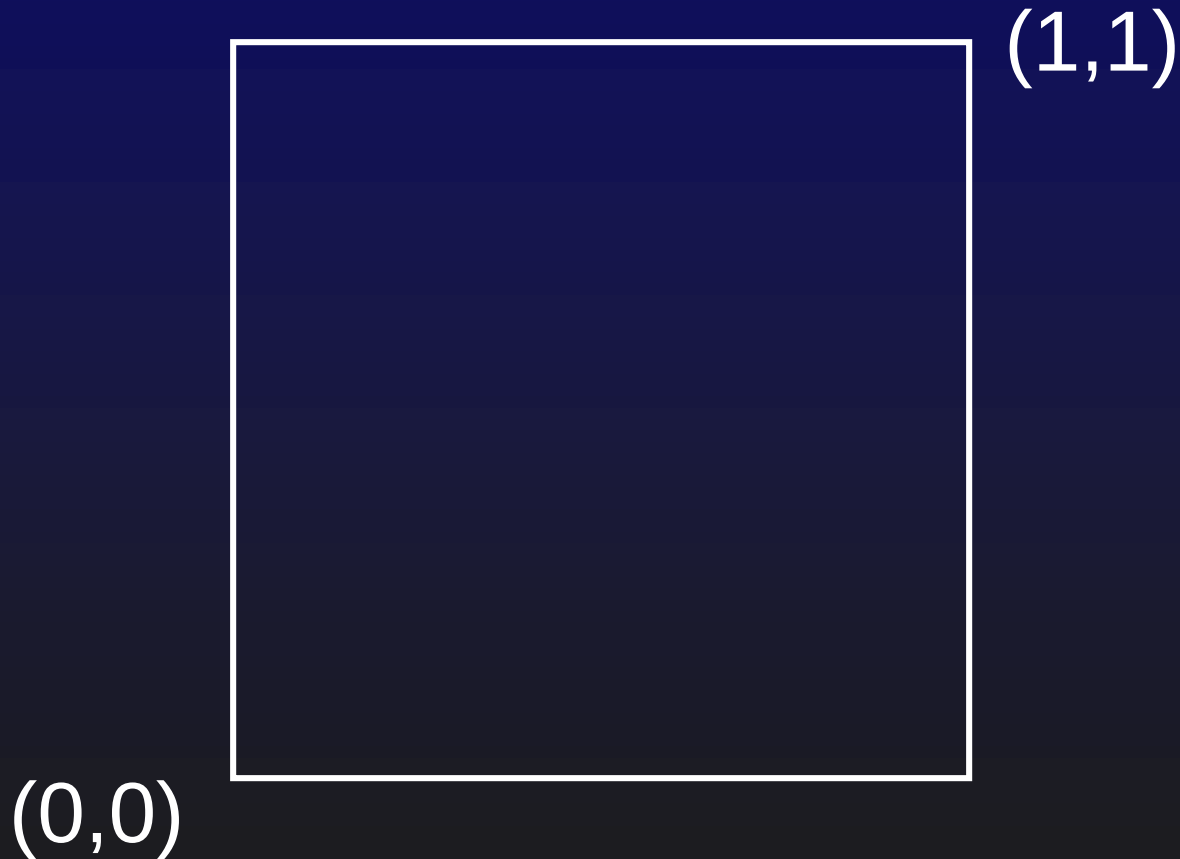
DEMO

SHOW 2D DEMOS



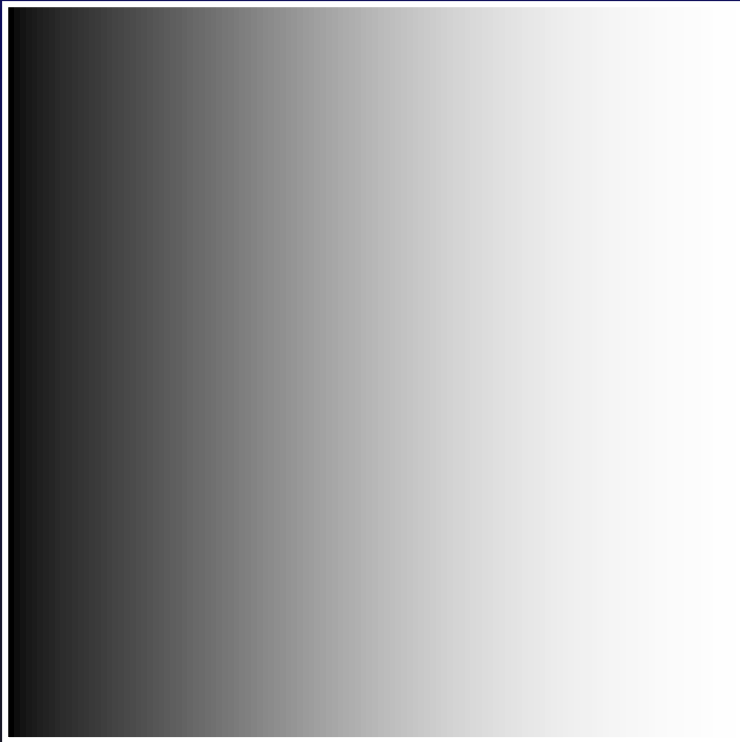
LIQUID TEXTURES

ANIMATE TEXTURE COORDINATES

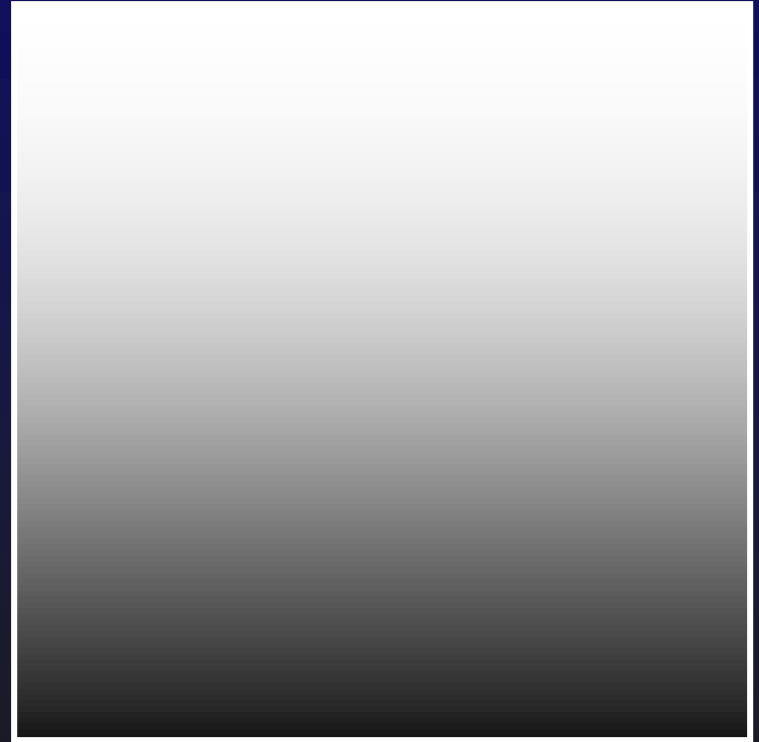


LIQUID TEXTURES

TREAT TEXTURE COORDINATE AS A DENSITY

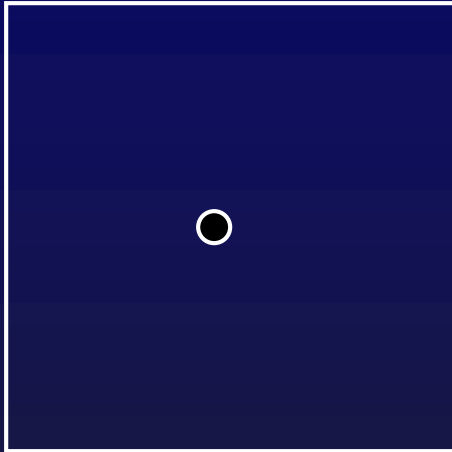


U-COORDINATE

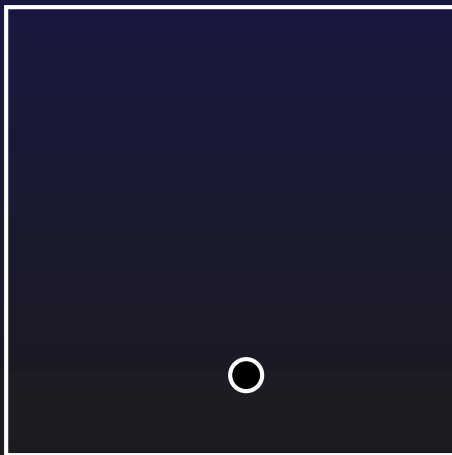


V-COORDINATE

LIQUID TEXTURES



(0.5,0.5)

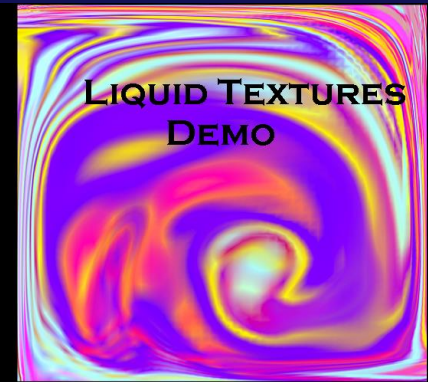


(0.2,0.52)

LIQUID TEXTURES

```
void tex_step ()  
{  
    SWAP(u_tex,u0_tex); SWAP(v_tex,v0_tex);  
    advect(u_tex,u0_tex,u,v);  
    advect(v_tex,v0_tex,u,v);  
}
```

DEMO

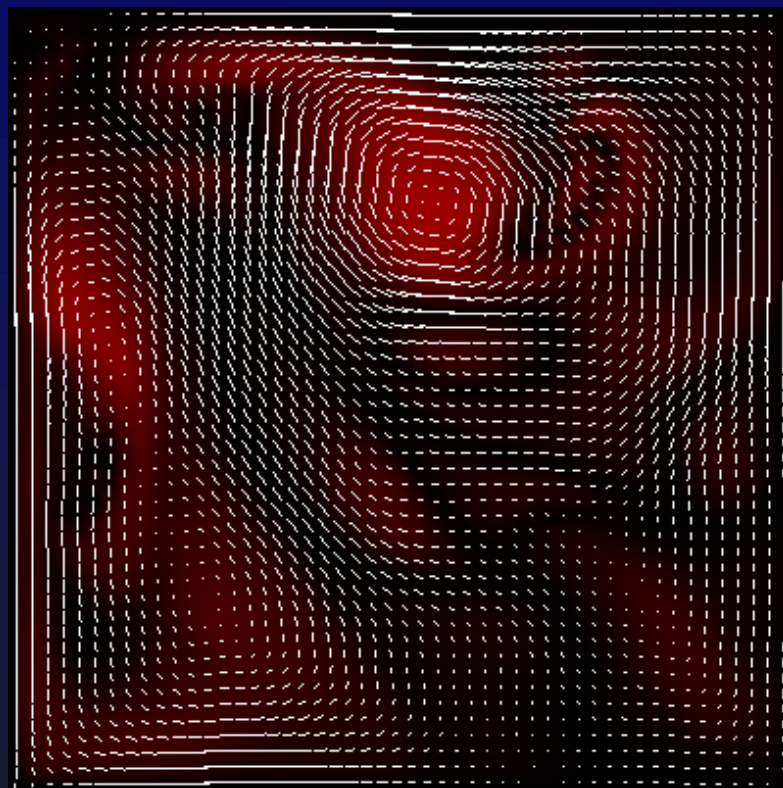


VORTICITY CONFINEMENT

TECHNIQUE TO DEFEAT DISSIPATION

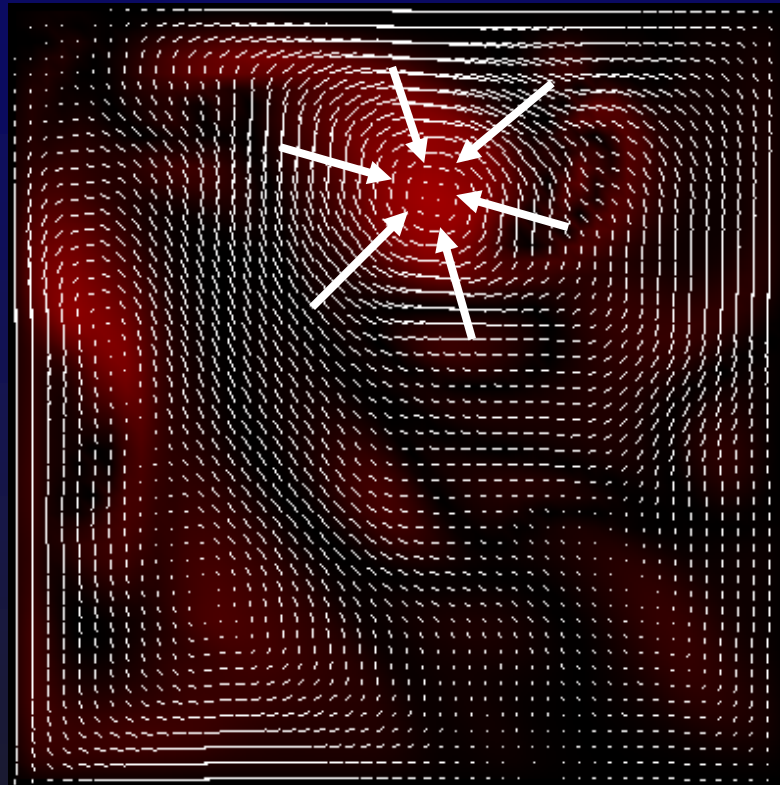
- STEINHOFF, *PHYSICS OF FLUIDS*, 1994.
- FEDKIW, STAM & JENSEN, *SIGGRAPH*, 2001.

VORTICITY CONFINEMENT



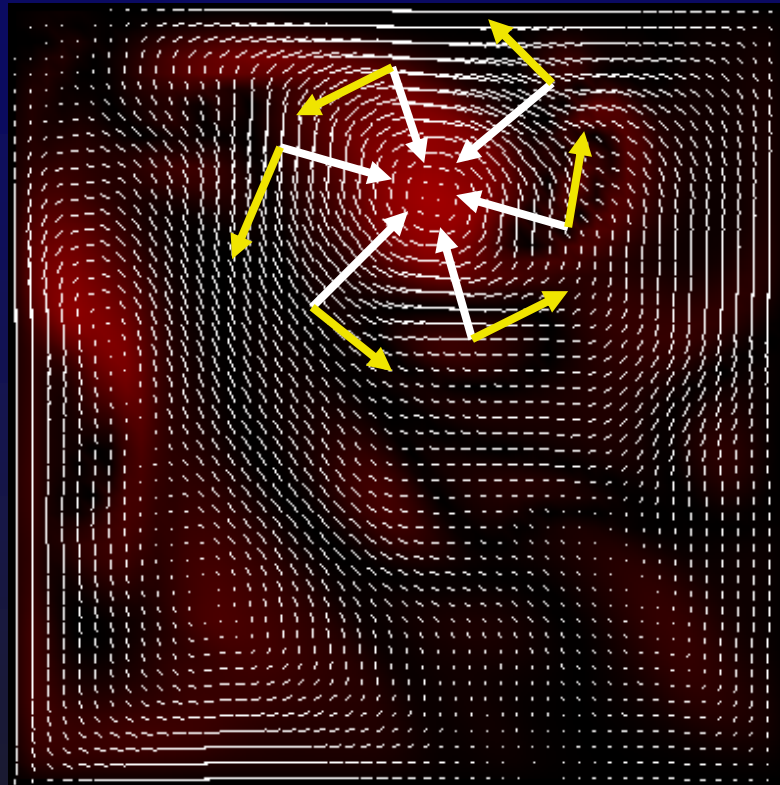
$$\omega = \nabla \times \mathbf{u}$$

VORTICITY CONFINEMENT



COMPUTE GRADIENT OF VORTICITY

VORTICITY CONFINEMENT



**ADD FORCE PERPENDICULAR TO THE
GRADIENT**

DEMO

VORTICITY CONFINEMENT DEMO

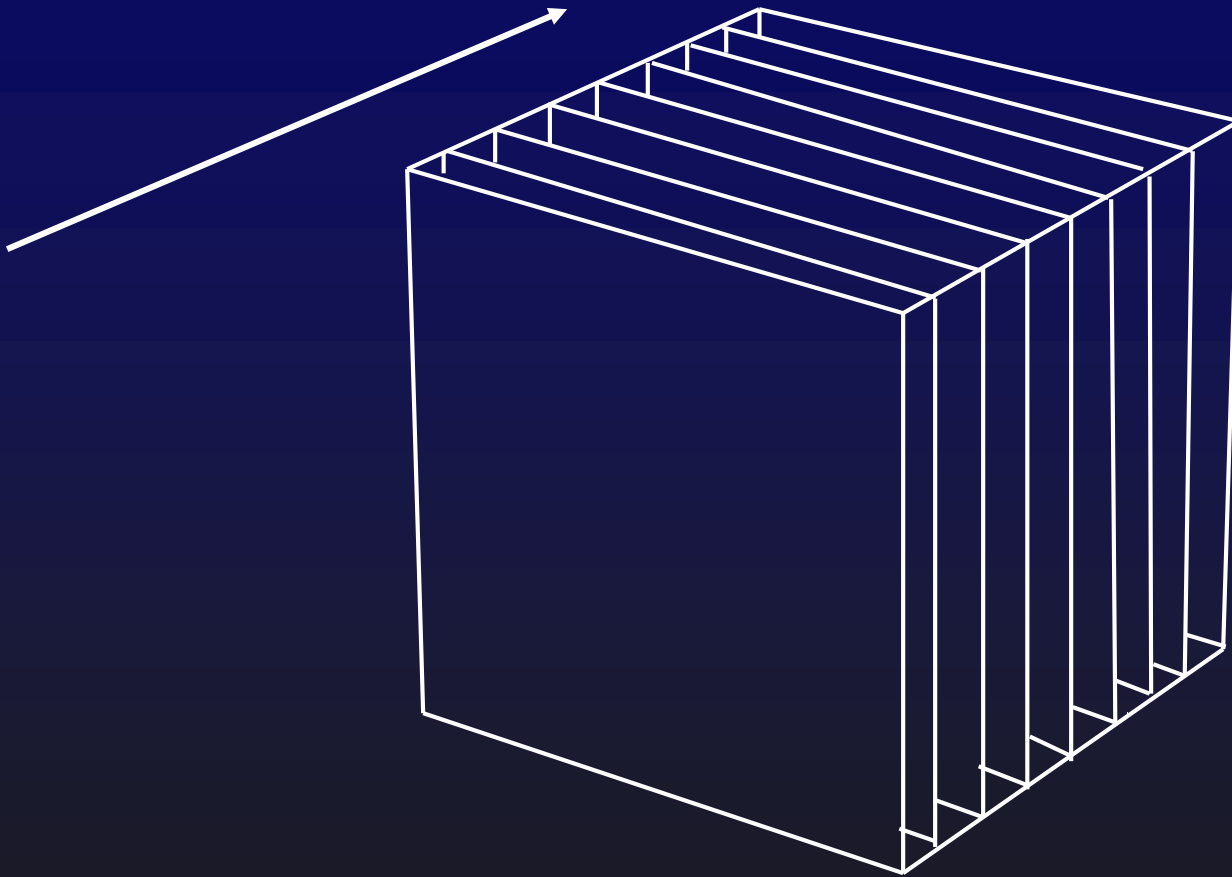
3D SOLVER

```
for ( i=1 ; i<=N ; i++ ) {  
    for ( j=1 ; j<=N ; j++ ) {  
        density[i,j] = ...  
    }  
}
```

BECOMES...

```
for ( i=1 ; i<=N ; i++ ) {  
    for ( j=1 ; j<=N ; j++ ) {  
        for ( k=1 ; k<=N ; k++ ) {  
            density[i,j,k] = ...  
        }  
    }  
}
```

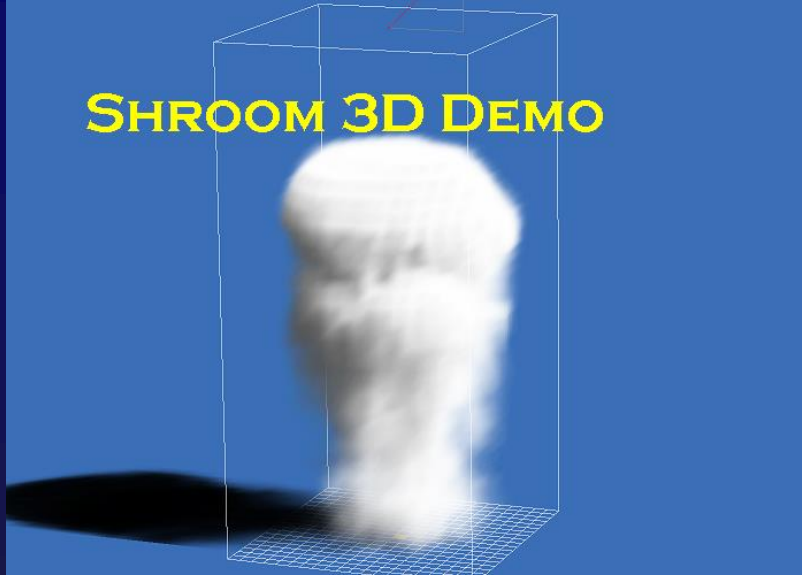
3D SOLVER



VOLUME RENDER DENSITY

DEMO

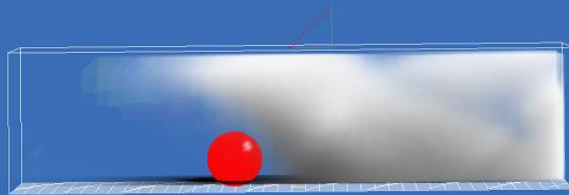
SHROOM 3D DEMO



3D FALLING BALL DEMO



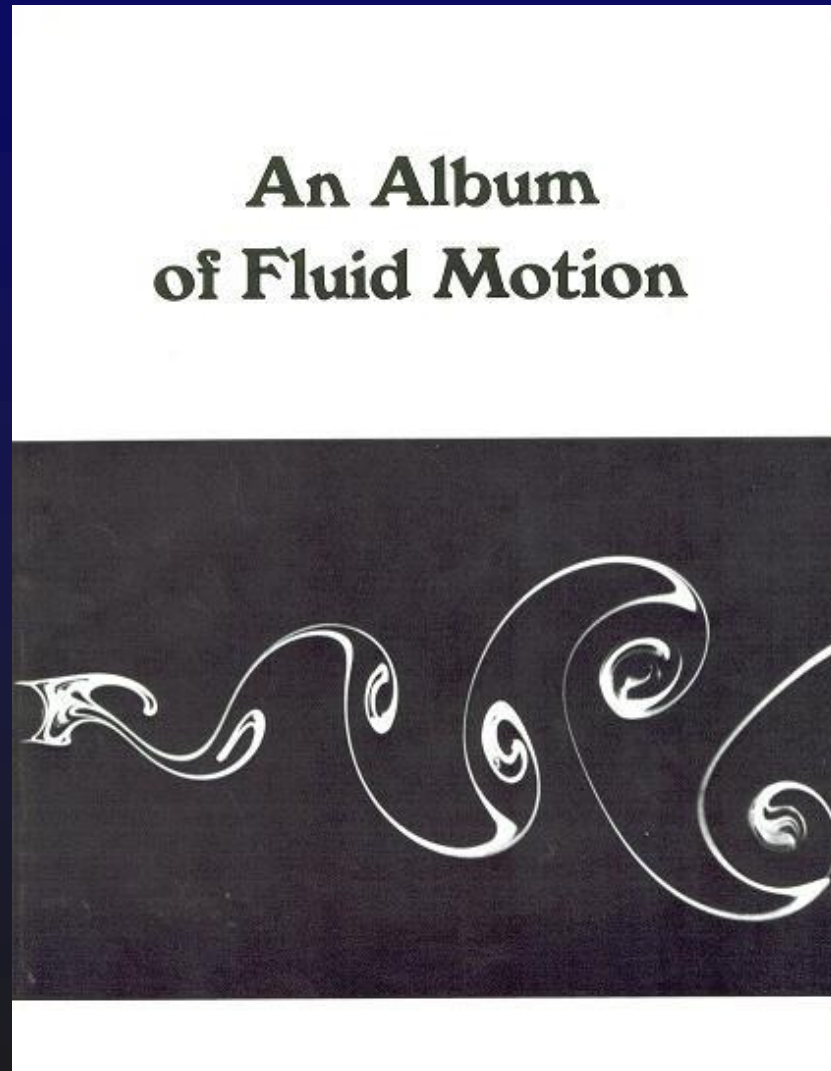
3D ROLLING BALL DEMO



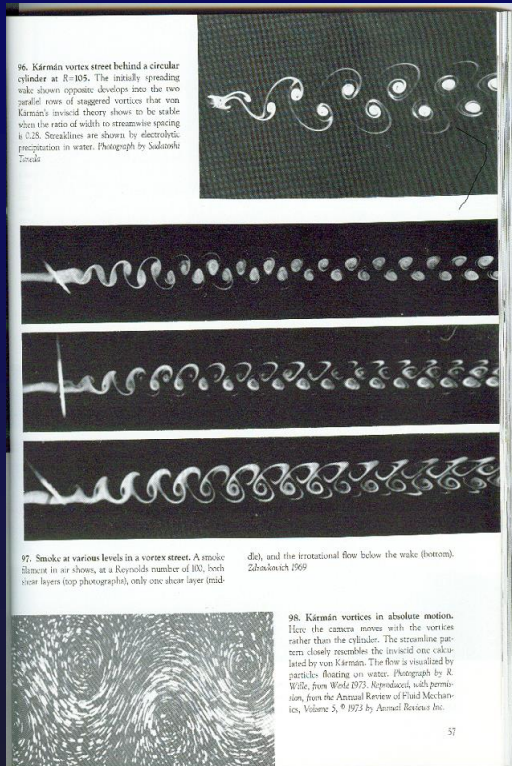
3D EXPLOSION DEMO



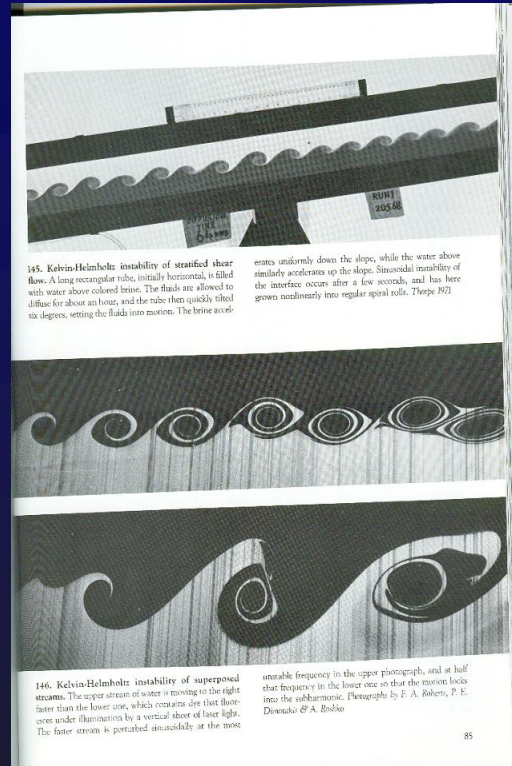
AN ALBUM OF FLUID MOTION



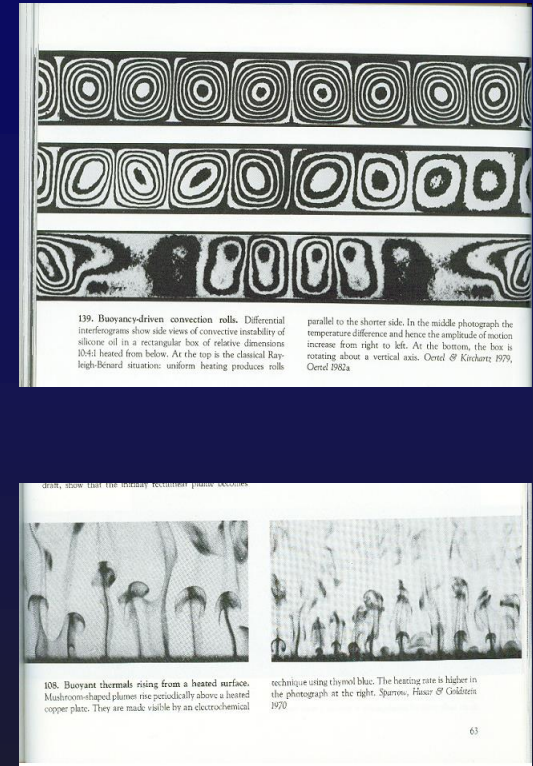
AN ALBUM OF FLUID MOTION



VON KARMANN



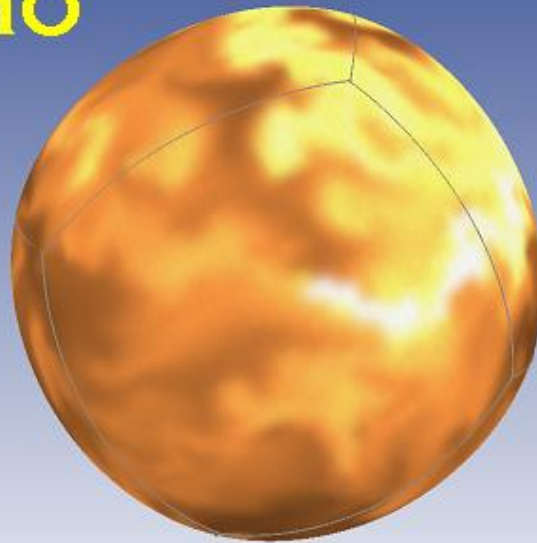
KELVIN-HELMHOLTZ



RAYLEIGH-BENARD

FLOWS ON SURFACES

CATMULL-CLARK FLUID DEMO



FLUIDS ON PDAs

FIXED POINT MATH:

8 BITS . **8 BITS**

```
#define freal short      // 16 bits
```

```
#define X1 (1<<8)
```

```
#define I2X(i) ((i)<<8)
```

```
#define X2I(x) ((x)>>8)
```

```
#define F2X(f) ((f)*X1)
```

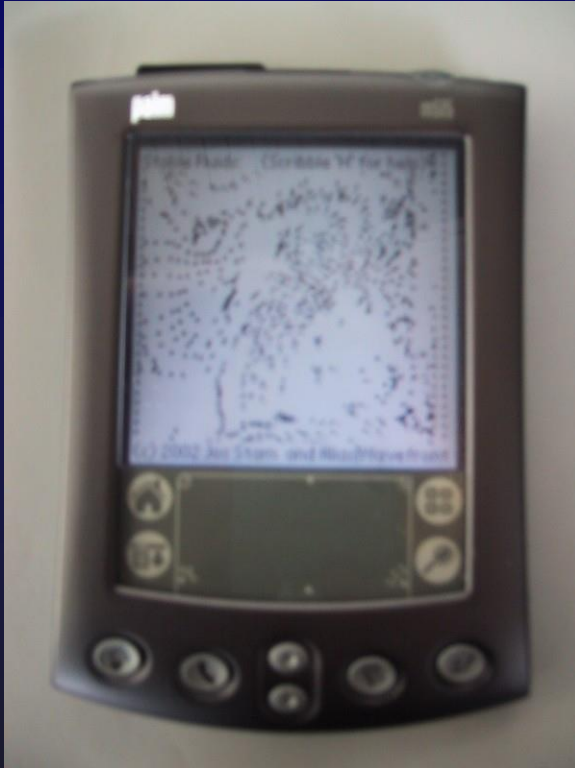
```
#define X2F(x) ((float)(x)/(float)X1)
```

```
#define XM(x,y) ((freal)((long)(x)*(long)(y))>>8)
```

```
#define XD(x,y) ((freal)((long)(x)<<8)/(long)(y))
```

```
x = a*(b/c)           x = XM(a,XD(b,c))
```

FLUIDS ON PDAs



PALM



POCKETPC

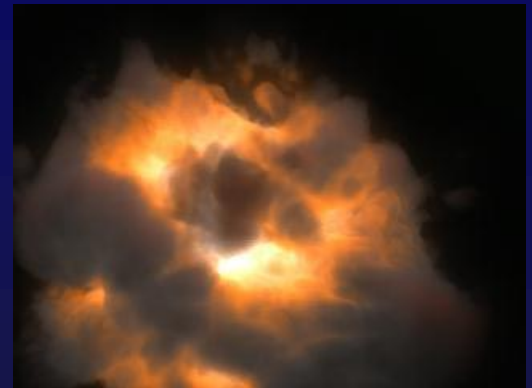
MAYA FLUID EFFECTS

**FLUID SOLVER NOW AVAILABLE
IN MAYA 4.5 UNLIMITED**

DOWNLOAD THE SCREENSAVER

<http://www.aliaswavefront.com>

MAYA FLUID EFFECTS



FUTURE WORK

- REAL-TIME WATER
- OUT OF THE BOX
- SMART TEXTURE MAPS
- (...)

